

NEW  
MATHEMATICS  
(TEACHER GUIDE)

Class Seven

**Chapter 1****SETS****Exercise:1.1**

1) Which of the following are sets?

i) The twelve months of a year.

**Solution:**

➤ Set. Ans

2) The team of cricketers of your school.

**Solution:**

➤ Set. Ans

3) The beautiful utensils.

**Solution:**

➤ Not a set. Ans

4) Best books.

**Solution:**

➤ Not a set. Ans

5) Prime numbers.

**Solution:**

➤ Set. Ans

2) Which of the following are sets?

i)  $A = \{ a, b, c \}$

➤ Set. Ans

ii)  $E = \{ \text{Beautiful birds} \}$

➤ Not a set. Ans

iii)  $B = \{ \text{Intelligent girls} \}$

➤ Not a set. Ans

iv)  $F = \{ 0, 1, 2, -1, -2, 0 \}$

➤ Set. Ans

v)  $C = \{ 1, 2, 3, 4, 5, \}$

➤ Set. Ans

3) Fill in the following blanks write  $\in$  or  $\notin$  to make a true statement.

- $12 \underline{\in} \{2, 4, 6, 8\}$
- $12 \underline{\in} \{3, 6, 9, 12, 15\}$
- $-2 \underline{\in} \{-1, -2, -3, -4\}$
- $8 \underline{\notin} \{1, 3, 5, 9, 11\}$
- $a \underline{\notin} \{x, y, z\}$

4) If  $A = \{1, 2, 3, 4\}$  and  $B = \{3, 4, 5, 6\}$  then state which of the following are true:

i)	4 E A • True. Ans	ii)	S E A • True. Ans
iii)	S E B • False. Ans	iv)	6 E A • True Ans

5) Which of the following statements are true and which are false.

- The order of elements of a set does not matter.
  - True. Ans
- The number any sets are of the same kind.
  - True. Ans
- An object can be included in a set repeatedly.
  - False. Ans
- Elements of a set must well-defined and distinct.
  - True. Ans
- Any collection of objects is called a set.
  - False. Ans

**Exercise: 1.2**

**1)** Write the following sets in tabular form.

i) A = Set of first eight letters of the English alphabet.  
➤ A = { a, b, c, d, e, f, g, h }. Ans

ii) B = Set of first five positive prime numbers.  
➤ B = { 2, 3, 5, 7, 11 }. Ans

iii) C = Set of integers than -5 and less than 3.  
➤ C = { -4, -3, -2, -1, 0, 1, 2 }. Ans

iv) D = Set of divisors of 48.  
➤ D = {1, 2, 3, 4, 5, 6, 7, 8, 12, 24, 48 }. Ans

v) E = Set of multiples of 3.  
➤ E = {3, 6, 9, 12..... }. Ans

**2)** Write the following sets in descriptive form.

1) A = { 1, 2, 3, 4, 5 }  
➤ A={Set of first five natural numbers}Ans

2) D= { 2, 4, 6, 8, 10}  
➤ D={Set of first five positive even numbers}  
Ans

3) E = { 2, 3, 5, 7, 11}  
➤ D={Set of first five positive prime numbers}  
Ans

4) H= { a, e, i, o, u}  
➤ H={Set of vowels of English alphabets } Ans

5) J = { 1,2,3.....}  
➤ J={Set of natural numbers } Ans

**3)** Which of the following sets have a finite or infinite number of elements.

1) A = { 8, 16, 24, 32.....}

- Infinite. Ans
- 2)  $B = \{ -10, -8, -6, -4, -2 \}$
- Finite. Ans
- 3)  $C = \{ 9, 12, 15, 18, 21, 24, 27 \}$
- Finite. Ans
- 4)  $W = \{ 0, 1, 2, 3, \dots \}$
- Infinite. Ans
- 5)  $X = \{ \dots, -4, -3, -2, 1, 2, 3, 4, \dots \}$
- Infinite. Ans
- 4) Which of the following are empty sets:
  - 1) The set of names of all these children who are the at the same time students of class VI and class VII
  - Empty Set. Ans
  - 2) The set of even numbers which are also even.
  - Empty Set. Ans
  - 3) The set of prime numbers which are also even.
  - No Empty Set. Ans
  - 4) The set of such composite numbers which are also odd
  - No Empty Set. Ans
  - 5) The set such years which have 13 months.
  - Empty Set. Ans

### Exercise 1.3

Find the union and intersection of the following pairs of set.

- 1)  $A = \{ 4, 5, 6 \}$  and  $B = \{ 4, 6, 8, 10 \}$

**Solution:**

- $A \cup B = \{4, 5, 6, 8, 10\}$ ,  $A \cap B = \{4, 6\}$  Ans
- 2)  $A = \{0, 1, 2, 3, 4\}$  and  $B = \{2, 4, 6, 8\}$
- **Solution**  
 $A \cup B = \{0, 1, 2, 3, 4, 6, 8\}$ ,  $A \cap B = \{2, 4\}$  Ans
- 3)  $A = \{1, 3, 5, 9, 11\}$  and  $B = \{1, 3, 5, 7, 11\}$

**Solution:**

- $A \cup B = \{1, 3, 5, 7, 9, 11\}$ ,  $A \cap B = \{1, 3, 5, 11\}$  Ans
- 4)  $A = \{a, b, c, d, e\}$  and  $B = \{a, e, i, o, u\}$

**Solution:**

- $A \cup B = \{A, b, c, d, e, I, o, u\}$ ,  $A \cap B = \{a, e\}$  Ans
- 5)  $A = \{\text{Sunday, Monday, Tuesday, Wednesday, Thursday, Friday, Saturday}\}$

**Solution:**

- $A \cup B = \{\text{Monday, Tuesday, Wednesday, Thursday, Friday, Saturday, Sunday}\}$   
 $A \cap B = \{\text{Wednesday, Thursday}\}$ . Ans
- 6)  $A = \{\text{set of first eight multiples of } t\}$  and  $B = \{\text{set of first six multiples of } 3\}$ .

**Solution:**

- $A \cup B = \{2, 3, 4, 6, 8, 9, 10, 12, 15, 16, 18\}$   
 $A \cap B = \{6, 12\}$ . Ans
- 7)  $A = \{\text{Set of first five positive even numbers}\}$   
and  $B = \{\text{set of first five natural numbers}\}$

**Solution:**

- $A \cup B = \{1, 2, 3, 4, 5, 6, 7, 8, 10\}$   $A \cap B = \{2, 4\}$  Ans
- 8)  $A = \{\text{Set of first five prime numbers}\}$  and  
 $B = \{\text{Set of first ten natural numbers}\}$ .

**Solution:**

➤  $A \cup B = \{1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11\}$   
 $A \cap B = \{2, 3, 5, 7\}$  Ans

9) If  $A = \{1, 2, 3, 4, 5, 6, 7, 8\}$ ,  $B = \{1, 3, 4, 7\}$  and  
 $C = \{2, 4, 6, 8\}$

The find the following sets:

1) $A \cup B$ <u><b>Solution</b></u> $\{1, 2, 3, 4, 5, 6, 7, 8\}$ Ans	2) $A \cup B$ <u><b>Solution</b></u> $\{7, 2, 3, 4, 5, 6, 7, 8\}$ Ans
3) $B \cup C$ <u><b>Solution</b></u> $\{1, 2, 3, 4, 5, 6, 7, 8\}$ Ans	4) $B \cup A$ <u><b>Solution</b></u> $\{1, 2, 3, 4, 5, 6, 7, 8\}$ Ans
5) $C \cup A$ <u><b>Solution</b></u> $\{1, 2, 3, 4, 5, 6, 7, 8\}$ Ans	6) $A \cap B$ <u><b>Solution</b></u> $\{1, 3, 5, 7\}$ Ans
7) $A \cap C$ <u><b>Solution</b></u> $\{2, 4, 6, 8\}$ Ans	8) $B \cap C$ <u><b>Solution</b></u> $\emptyset$ Ans
9) $B \cap A$ <u><b>Solution</b></u> $\{1, 3, 5, 7\}$ Ans	10) $C \cap A$ <u><b>Solution</b></u> $\{2, 4, 6, 8\}$ Ans

Q.10: If  $A = \{ 2, 3, 6, 8 \}$  and  $B = \{ a, b, c, d \}$ , then verify.

i)  $A \cup B = B \cup A$

ii)  $A \cap B = B \cap A$

iii)  $A \cup B = B \cup A$

Solution:

Take LHS

$$A \cup B = \{ 2, 3, 6, 8 \} \cup \{ a, b, c, d \}$$

$$A \cup B = \{ 2, 3, 6, 8, a, b, c, d \}$$

Take RHS

$$B \cup A = \{ a, b, c, d \} \cup \{ 2, 3, 6, 8 \}$$

$$B \cup A = \{ 2, 3, 6, 8, a, b, c, d \}$$

Hence proved  $A \cup B = B \cup A$ .

ii)  $A \cap B = B \cap A$

Solution:

Take LHS

$$A \cap B = \{ 2, 3, 6, 8 \} \cap \{ a, b, c, d \}$$

$$A \cap B = \{ \emptyset \}$$

Take RHS

$$B \cap A = \{ a, b, c, d \} \cap \{ 2, 3, 6, 8 \}$$

$$B \cap A = \{ \emptyset \}$$

Hence proved

$$A \cap B = B \cap A$$

**Chapter 2****THE SYSTEM OF RATIONAL NUMBERS****Exercise 2.1****And its Evaluation**

1) Find the rational number.

**Solution:**

Any number of the form  $\frac{p}{q}$  is a rational number. Ans.

2) Which of the following are rational numbers?

**Solution:**

Are all rational numbers Ans

3) Classify the following as positive or negative rational numbers.

1)  $\frac{3}{5}$   
Positive  
Ans

3)  $-\frac{3}{13}$   
Positive  
Ans

5)  $-\left(\frac{-7}{9}\right)$   
Negative  
Ans

2)  $\frac{-6}{-7}$   
Positive  
Ans

4)  $\frac{5}{-6}$   
Negative  
Ans

6)  $\left(\frac{8}{-15}\right)$   
Positive  
Ans

7) $\frac{6}{13}$ Negative Ans	8) $\frac{89}{-11}$ Negative Ans
9) $\frac{-12}{17}$ Negative Ans	10) $\frac{-4}{5}$ Negative Ans

4) Write down the first five negative integers as rational numbers.

$$\frac{-1}{1}, \frac{-2}{1}, \frac{-3}{1}, \frac{-4}{1}, \text{ and } \frac{-5}{1} \text{ Ans}$$

5) Write down the positive integers blw 19 and 25 as rational numbers.

**Solution:**

$$\frac{20}{1}, \frac{21}{1}, \frac{22}{1}, \frac{23}{1}, \frac{24}{1} \text{ Ans}$$

6) Express  $\frac{3}{6}, \frac{-10}{15}, \frac{-75}{125}$ , and  $\frac{-18}{63}$  in standard form.

**Solution:**

$$\frac{1}{2}, \frac{-2}{3}, \frac{2}{5}, \frac{3}{5}, \frac{-2}{7} \text{ Ans}$$

7) write down the opposites of following rational.

$$\text{Numbers. } \frac{3}{7}, -5\frac{1}{2}, 6.2, \frac{-5}{-6}, \frac{12}{-17}$$

**Solution:**

$$\frac{-3}{7}, -5\frac{-2}{1}, 6.2, \quad \frac{-5}{6}, \frac{12}{17} \quad \text{Ans}$$

8) Which of the following statements are true?

1) Every natural number is the rational number.  
⇒ T Ans

2) 0 is not a rational number.  
F Ans

3) Fractions are not rational number.  
⇒ F Ans

4)  $\frac{2}{3}, \frac{+2}{+3}, \frac{-2}{-3}$  are all one and the same rational number.  
⇒ T Ans

5) Every rational number can be represented with a positive denominator  
⇒ F Ans

6) The rational number  $\frac{3}{-10}$  is in standard form.  
⇒ F Ans

7)  $\frac{3}{0}$  is a rational number  
⇒ F Ans

8) Every integers can be represented as a rational number.  
⇒ T Ans

**Exercise 2.2**

1) Given below are pairs of rational numbers.  
Pick out the equal pairs.

1)  $\frac{-15}{-20}, \frac{-16}{-24}$

2)  $\frac{16}{-20}, \frac{20}{-25}$

**Solution:**

⇒ Not equal Pairs.  
Ans

**Solution:**

⇒ Equal pairs.  
Ans

3)  $\frac{-7}{21}, \frac{-6}{13}$

4)  $\frac{-8}{-20}, \frac{6}{15}$

**Solution:**

⇒ Not equal Pair.  
Ans

**Solution:**

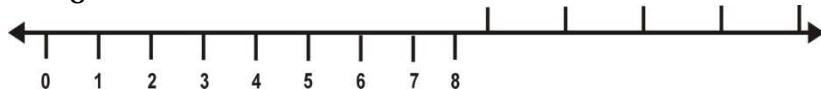
⇒ Equal pairs.  
Ans

5)  $\frac{-7}{15}, \frac{-6}{13}$

**Solution:**  
⇒ Not equal Pairs.  
Ans

2) Represent the following numbers on a number – line.

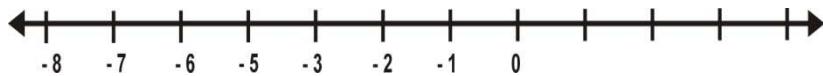
1)  $\frac{5}{8}$



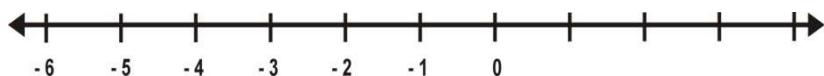
2)  $\frac{3}{4}$



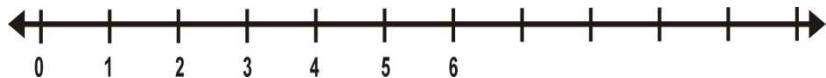
3)  $\frac{3}{8}$



4)  $\frac{5}{6}$



5)  $\frac{3}{6}$



Q.3: State whether the following statements are true or false.

- i) Rational number  $\frac{2}{3}$  and  $\frac{3}{3}$  represented the same integer 1. T
- ii) Rational numbers  $\frac{0}{3}$  lies to right of 0. F
- iii) Rational numbers  $\frac{-2}{5}$  and  $\frac{2}{5}$  are equidistant from 0 but on opposite sides of it. T
- iv) Rational numbers  $\frac{-3}{3}$  and  $\frac{-4}{4}$  represent same integer 1. T
- v) Rational numbers  $\frac{4}{2}$  and  $\frac{6}{3}$  do not represent the same integer. F

### Exercise 2.3

1) Arrange the rational number  $\frac{-3}{4}$ ,  $\frac{4}{-5}$ ,  $\frac{-3}{2}$ ,

$\frac{2}{-3}$  and 0 in the ascending order.

**Solution:**

$$\Rightarrow \frac{-3}{2}, \frac{4}{5}, \frac{-3}{4}, \frac{2}{-3}, 0 \quad \text{Ans}$$

2) Arrange the rational numbers  $\frac{3}{4}, \frac{-4}{-5}, \frac{-3}{2}$   
 $\frac{-2}{3}$  and 0 in the ascending order.

**Solution:**

$$\Rightarrow \frac{2}{3}, \frac{-4}{-5}, \frac{3}{4}, \frac{-3}{2}, 0 \quad \text{Ans}$$

3) Write following integers as rational numbers  
 $0, -3, 12, 25, -100$ .

**Solution:**

$$\Rightarrow \frac{0}{1}, \frac{-3}{1}, \frac{12}{1}, \frac{25}{1}, \frac{100}{1} \quad \text{Ans}$$

4) Write the rational numbers equal to  $\frac{4}{5}$   
 Whose denominators are 12, 20 and 32.

**Solution:**

$$\Rightarrow \frac{12}{15}, \frac{20}{25}, \frac{32}{40} \quad \text{Ans}$$

5) Write three rational numbers equal of  $\frac{60}{90}$   
 Whose whose denominators are 30, 15, and  
 3respectively.

**Solution:**

$$\Rightarrow \frac{20}{30}, \frac{10}{25}, \frac{32}{40} \quad \text{Ans}$$

6) List five rational numbers which are not  
 fraction.



2) Verify the property  $|x| + |y| \leq |x + y|$  for the following value of  $x$  and  $y$ .

1)  $\frac{-3}{7}, \frac{1}{2}$

**Solution:**

$$\Rightarrow |x + y| = \left| -\frac{3}{4} + \frac{1}{2} \right| = -\frac{1}{4}$$

$$|x| + |y| = \left| -\frac{3}{4} \right| + \left| \frac{1}{2} \right| = \frac{3}{4} + \frac{1}{2} = \frac{5}{4}$$

Since  $\frac{1}{4} \leq \frac{5}{4}$ , the inequality holds Ans

2)  $\frac{2}{5}, \frac{1}{3}$

**Solution:**

$$\Rightarrow |x + y| = \left| \frac{2}{5} + \frac{1}{3} \right| = \frac{11}{15}$$

$$|x| + |y| = \left| \frac{2}{5} \right| + \left| \frac{1}{3} \right| = \frac{2}{5} + \frac{1}{3} = \frac{11}{15}$$

Since  $\frac{11}{15} \leq \frac{11}{15}$ , the inequality holds Ans

3)  $\frac{1}{8}, \frac{-3}{7}$

**Solution:**

$$\Rightarrow |x + y| = \left| \frac{1}{8} - \frac{3}{7} \right| = \left| -\frac{17}{56} \right| = \frac{17}{56}$$

$$|x| + |y| = \left| \frac{1}{8} \right| + \left| \frac{-3}{7} \right| = \left| -\frac{3}{7} \right| = \frac{1}{8} + \frac{3}{7} = \frac{31}{56}$$

Since  $\frac{17}{56} \leq \frac{31}{56}$ , the inequality holds Ans

4) 
$$\begin{array}{r} -5 \\ -13 \\ \hline \end{array}$$

Solution:

$$\Rightarrow |x + y| = | -\frac{2}{3} - \frac{1}{3}| = |-1| = 1$$

$$|x| + |y| = | -\frac{3}{3}| + | -\frac{1}{3}| = \frac{2}{3} + \frac{1}{3} = 1 \quad \text{Ans}$$

3) verify the property  $|x| = |-x|$  for the following values of x and y.

1) 
$$\begin{array}{r} 3 \\ 7 \\ \hline \end{array}$$

Solution:

$$x = \frac{3}{7}$$

$$|x| = |\frac{3}{7}| = \frac{3}{7}$$

$$|-x| = | -\frac{3}{7}| = \frac{3}{7} \text{ . equality holds.} \quad \text{Ans}$$

2) 
$$\begin{array}{r} -1 \\ 11 \\ \hline \end{array}$$

Solution:

$$\Rightarrow x = \frac{-1}{11}$$

$$|x| = | -\frac{1}{11}| = \frac{1}{11}$$

$$|-x| = | \frac{1}{11}| = \frac{1}{11} = \text{the equality holds.} \quad \text{Ans}$$

$$3) \quad \begin{array}{r} 7 \\ -15 \\ \hline \end{array}$$

Solution:

$$\Rightarrow x = \frac{7}{15}$$

$$|x| = \left| \frac{7}{15} \right| = \frac{7}{15}$$

$|-x| = \left| \frac{-7}{15} \right| = \frac{7}{15}$  = the equality hole. Ans

$$4) \quad \begin{array}{r} -5 \\ -13 \\ \hline \end{array}$$

Solution:

$$x = \frac{-5}{-13}$$

$$|x| = \left| \frac{5}{13} \right| = \frac{5}{13}$$

$|-x| = \left| \frac{-5}{13} \right| = \frac{5}{13}$  = the equality hole. Ans

## Chapter 3

## SQUARE ROOT

Exercise 3.1

Q.1 Find the square roots of the following.

1) 196

Soltuion:

$$\begin{array}{r|rr}
 2 & 196 \\
 \hline
 2 & 98 \\
 \hline
 7 & 49 \\
 \hline
 7 & 7 \\
 \hline
 & 1
 \end{array}$$

$$= \sqrt{196}$$

$$= \sqrt{2 \times 2 \times 7 \times 7}$$

$$= 2 \times 7$$

$$= 14 \quad \text{Ans}$$

2) 625

Soltuion:

$$\begin{array}{r|rr}
 5 & 625 \\
 \hline
 5 & 125 \\
 \hline
 5 & 25 \\
 \hline
 5 & 5 \\
 \hline
 & 1
 \end{array}$$

$$= \sqrt{625}$$

$$= \sqrt{5 \times 5 \times 5 \times 5}$$

$$= 5 \times 5$$

$$= 25 \quad \text{Ans}$$

3) 289

Soltuion:

$$\begin{array}{r|rr}
 17 & 289 \\
 \hline
 17 & 17 \\
 \hline
 & 1
 \end{array}$$

$$= \sqrt{289}$$

$$= \sqrt{17 \times 17}$$

$$= 17 \quad \text{Ans}$$

4) 841

Soltuion:

$$\begin{array}{r|rr}
 29 & 841 \\
 \hline
 29 & 29 \\
 \hline
 & 1
 \end{array}$$

$$= \sqrt{841}$$

$$= \sqrt{29 \times 29}$$

$$= 29 \quad \text{Ans}$$

5) 1521

Soltuion:

3	1521
3	507
13	169
13	13
	1

$$= \sqrt{1521}$$

$$= \sqrt{3 \times 3 \times 13 \times 13}$$

$$= 3 \times 13$$

$$= 39 \quad \text{Ans}$$

7) 1600

Soltuion:

2	1600
2	800
2	400
2	200
2	100
2	50
5	25
5	5
	1

$$= \sqrt{1600}$$

$$= \sqrt{2 \times 2 \times 2 \times 2 \times 2 \times 5 \times 5}$$

$$= 2 \times 2 \times 2 \times 5$$

$$= 40 \quad \text{Ans}$$

6) 3025

Soltuion:

5	3025
5	605
11	121
11	11
	1

$$= \sqrt{3025}$$

$$= \sqrt{5 \times 5 \times 11 \times 11}$$

$$= 5 \times 11$$

$$= 55 \quad \text{Ans}$$

8) 4225

Soltuion:

5	4225
5	845
13	169
13	13
	1

$$= \sqrt{4225}$$

$$= \sqrt{5 \times 5 \times 13 \times 13}$$

$$= 5 \times 13$$

$$= 65 \quad \text{Ans}$$

9) 4900

Soltuion:

7	4900
7	700
2	100
2	50
5	25
5	5
	1

$$= \sqrt{4900}$$

$$= \sqrt{7 \times 7 \times 2 \times 2 \times 5 \times 5}$$

$$= 7 \times 2 \times 5$$

$$= 70 \quad \text{Ans}$$

10) 2916

Soltuion:

2	2916
2	1458
3	729
3	243
3	81
3	27
3	9
3	3
	1

$$= \sqrt{2916}$$

$$= \sqrt{2 \times 2 \times 3 \times 3 \times 3 \times 3 \times 3}$$

$$= 3 \times 3 \times 3 \times 3$$

$$= 54 \quad \text{Ans}$$

11)  $2 \frac{4}{16}$

Soltuion:

$$\frac{36}{16}$$

$$= \sqrt{36}$$

$$16$$

$$= \sqrt{2 \times 2 \times 3 \times 3}$$

$$= \frac{2 \times 3}{2 \times 2}$$

2	36
2	18
3	9
3	3
	1

5	4225
5	845
13	169
13	13
	1

$$= \frac{6}{4} \quad \text{Ans}$$

12)  $\frac{484}{169}$

Soltuion:

$$\begin{array}{c|c}
 2 & 484 \\
 \hline
 2 & 242 \\
 \hline
 11 & 121 \\
 \hline
 11 & 11 \\
 \hline
 & 1
 \end{array}
 \quad
 \begin{array}{c|c}
 13 & 169 \\
 \hline
 13 & 13 \\
 \hline
 & 1
 \end{array}$$

$$\begin{array}{l}
 = \sqrt{484} \\
 = \sqrt{2 \times 2 \times 11 \times 11} \\
 = \frac{2 \times 11}{13} = \frac{22}{13} \text{ Ans}
 \end{array}$$

$$169 \quad 13 \times 13$$

13) 6724

Soltuion:

$$\begin{array}{c|c}
 2 & 1521 \\
 \hline
 2 & 3362 \\
 \hline
 41 & 1681 \\
 \hline
 41 & 41 \\
 \hline
 & 1
 \end{array}$$

$$\begin{aligned}
 &= \sqrt{6724} \\
 &= \sqrt{2 \times 2 \times 41 \times 41} \\
 &= 2 \times 41 \\
 &= 82 \quad \text{Ans}
 \end{aligned}$$

14) 7744

Soltuion:

$$\begin{array}{c|c}
 2 & 7744 \\
 \hline
 2 & 3872 \\
 \hline
 2 & 1936 \\
 \hline
 2 & 968 \\
 \hline
 2 & 484 \\
 \hline
 2 & 242 \\
 \hline
 11 & 121 \\
 \hline
 11 & 11 \\
 \hline
 & 1
 \end{array}$$

$$\begin{aligned}
 &= \sqrt{7744} \\
 &= \sqrt{2 \times 2 \times 2 \times 2 \times 2 \times 11 \times 11} \\
 &= 2 \times 2 \times 2 \times 11 \\
 &= 88 \quad \text{Ans}
 \end{aligned}$$

15) 9409

**Soltuion:**

$$\begin{array}{r|l} 97 & 9409 \\ \hline 97 & 97 \\ \hline & 1 \end{array}$$

$$= \sqrt{9409}$$

$$= \sqrt{97 \times 97}$$

$$= 97 \text{ Ans}$$

**Exercise 3.2**

Q.1 In a party 625 chairs were arranged in such a way that there were as many chairs in each row as the number of rows. Find the number of chairs in each row.

**Soltuion:**

$$\begin{array}{r|l} 5 & 625 \\ \hline 5 & 125 \\ \hline 5 & 25 \\ \hline 5 & 5 \\ \hline & 1 \end{array}$$

$$= \sqrt{529}$$

$$= \sqrt{5 \times 5 \times 5 \times 5}$$

$$= 5 \times 5 = 25 \text{ Ans}$$

Q.2 A farmer planted 529 trees in a plot such that there were as many trees in each row as the number of rows. Find the number of trees in each row.

Solution:

$$\begin{array}{r|l}
 23 & 529 \\
 \hline
 23 & 23 \\
 \hline
 & 1
 \end{array}$$

$$\begin{aligned}
 &= \sqrt{529} \\
 &= \sqrt{23 \times 23} \\
 &= 23 \quad \text{Ans}
 \end{aligned}$$

Q.3 A gardener wishes to keep 676 flower-pots at equal distance on a square plot. How many pots should he keep in each row?

Solution:

$$\begin{array}{r|l}
 2 & 676 \\
 \hline
 2 & 338 \\
 \hline
 13 & 169 \\
 \hline
 13 & 13 \\
 \hline
 & 1
 \end{array}$$

$$\begin{aligned}
 &= \sqrt{676} \\
 &= \sqrt{2 \times 2 \times 13 \times 13} \\
 &= 2 \times 13 = 26 \quad \text{Ans}
 \end{aligned}$$

Q.4 Students of a school contributed as many paisas in Red cross fund, as the number of students present. If total contribution was Rs. 2500. Find the number of students present and amount contributed by each.

**Solution:**

$$\begin{array}{r|l}
 2 & 2500 \\
 \hline
 2 & 1250 \\
 \hline
 5 & 625 \\
 \hline
 5 & 125 \\
 \hline
 5 & 25 \\
 \hline
 5 & 5 \\
 \hline
 & 1
 \end{array}$$

$$\begin{aligned}
 &= \sqrt{2500} \\
 &= \sqrt{2 \times 2 \times 5 \times 5 \times 5 \times 5} \\
 &= 2 \times 5 \times 5 = 50 \quad \text{Ans}
 \end{aligned}$$

Q.5 Some girls plucked as many flowers each as total number of them. If the flower 529 find the number of girls.

$$\begin{array}{r|l}
 23 & 529 \\
 \hline
 23 & 23 \\
 \hline
 & 1
 \end{array}$$

$$\begin{aligned}
 &= \sqrt{529} \\
 &= \sqrt{23 \times 23} \\
 &= 23 \quad \text{Ans}
 \end{aligned}$$

**Q.6** Area of square field is 46656 square feet. Find the length of its sides.

**Solution:**

$$\begin{array}{r|rr}
 2 & 46656 \\
 \hline
 2 & 23328 \\
 \hline
 2 & 11664 \\
 \hline
 2 & 5832 \\
 \hline
 2 & 2916 \\
 \hline
 2 & 1458 \\
 \hline
 3 & 729 \\
 \hline
 3 & 243 \\
 \hline
 3 & 81 \\
 \hline
 3 & 27 \\
 \hline
 3 & 9 \\
 \hline
 3 & 3 \\
 \hline
 & 1
 \end{array}$$

$$= \sqrt{46656}$$

$$= \sqrt{2 \times 2 \times 2 \times 2 \times 2 \times 3 \times 3 \times 3 \times 3}$$

$$= 2 \times 2 \times 2 \times 2 \times 3 \times 3 \times 3 = 216 \quad \text{Ans}$$

**Q.7** A rectangular field had its length twice its breadth. If its area is 22050 square feet. Find its length and breadth.

First divide the 22050 by 2 –

Then,  $22050 \div 2 = 11025$

$$= \sqrt{11025} == \sqrt{3 \times 3 \times 5 \times 5 \times 7 \times 7}$$

$$= 3 \times 4 \times 7 = 105.$$

If the width is 105 feet. Since the length is double than width. Then multiply 105 by 2.  
 $105 \times 2$   
 $= 210$

The length of rectangular field is 210 feet.

Q.8 A P.T teacher wished to arranged his students to form a square with 29 students in each row and 22 students were left over. Find the total number of students.

**Solution:**

$$\begin{array}{r} 29 \times 29 \\ = 841 \end{array}$$

Now Add 22 in 841

$$\begin{array}{r} 841 \\ +22 \\ \hline 863 \end{array}$$

the total numbers of students = 863 Ans

Q.9 A drill master arranged of students to form a square with 22 students in each row. Was short of 14 students. Find the number of students.

**Solution:**

$$\begin{array}{r} = 22 \times 22 \\ = 484 \end{array}$$

Now subtract 14 from 484

$$\begin{array}{r} 484 \\ -14 \\ \hline 470 \end{array}$$

The number of students = 470 Ans

Q.10 An army officer ordered his group of 2025 soldiers to form a square and two places were left vacant. How many soldiers stood in each row?

**Solution:**

3	2025
3	675
3	225
3	75
5	25
5	5
	1

$$= \sqrt{2025}$$

$$= \sqrt{3 \times 3 \times 3 \times 3 \times 5 \times 5}$$

$$= 3 \times 3 \times 5 = 45 \text{ Ans}$$

### **Exercise 3.3**

1) Find the value of each of the following.

$$1) \quad \underline{\sqrt{25} - \sqrt{9}}$$

$$\underline{\sqrt{25} - \sqrt{9}}$$

**Solution:**

$$\sqrt{25} = 5, \sqrt{9} = 3$$

$$\frac{5-3}{5+3} = \frac{2}{8} = \frac{1}{4} \quad \text{Answer}$$

$$\begin{aligned}
 2) \quad & \frac{1}{\sqrt{30}} + \frac{1}{\sqrt{9}} \\
 \Rightarrow & \sqrt{36} - 6, \sqrt{9} = 3 \\
 & \frac{1}{6} + \frac{1}{3} + \frac{1}{0} + \frac{2}{6} = \frac{3}{6} = \frac{1}{2} \quad \text{Ans}
 \end{aligned}$$

$$\begin{aligned}
 3) \quad & (\sqrt{169} - 4)^2 \\
 \text{Solution:} \quad & \Rightarrow \sqrt{169} = 13 \\
 & (13 - 4)^2 = 9^2 = 81 \quad \text{Ans}
 \end{aligned}$$

$$\begin{aligned}
 4) \quad & 3(\sqrt{36} - 2)^2 \\
 \text{Solution:} \quad & \Rightarrow \sqrt{36} = 6 \\
 & 3(6 - 2)^2 = 3(4)^2 = 3(16) = 48 \quad \text{Ans}
 \end{aligned}$$

$$\begin{aligned}
 5) \quad & \sqrt{5\frac{1}{16}} - \sqrt{256} + \sqrt{12\frac{1}{4}} \\
 \text{Solution:} \quad & \sqrt{\frac{1}{16}} = \frac{1}{4}, \sqrt{256} = 1.6 \\
 & \sqrt{12\frac{1}{4}} = \sqrt{\frac{47}{4}} = \sqrt{\frac{47}{2}}
 \end{aligned}$$

$$\begin{aligned}
 & 5\left(\frac{1}{4}\right) - 1.6 + \sqrt{\frac{47}{2}} = 1.25 - 1.6 + \sqrt{\frac{47}{2}} \\
 & = 1.25 - 1.6 + 3.416 = 2.066 \quad \text{Ans}
 \end{aligned}$$

6)  $(\sqrt{81 - 3})^2$

Solution:

$$\Rightarrow \sqrt{81} = 9$$

$$(9 - 3)^2 = (6)^2 = 36 \quad \text{Ans}$$

7)  $(2 \frac{2}{5})^2 \times (\frac{5}{6})^2 - \sqrt{4}$

Solution:

$$\Rightarrow 2 \frac{2}{5} = \frac{12}{5}$$

$$(\frac{12}{5})^2 \times (\frac{5}{6})^2 - 2 = \frac{144}{25} \times \frac{25}{36} - 2 = 4 - 2 = 2 \quad \text{Ans}$$

8)  $3(\sqrt{36}) + 2((\sqrt{36}))$

Solution:

$$\Rightarrow \sqrt{36} = 6$$

$$3(6) + 2(6) = 18 + 12 = 30 \quad \text{Ans}$$

**Chapter 4****PERCENTAGE****Exercise 4.1**

Find profit or loss percent if:

1) C.P = Rs. 250 , S.P = Rs. 300

**Solution:**

$$\Rightarrow S.P - C.P = 300 - 250 = \text{Rs. } 50$$

$$\text{Profit percentage} = \frac{50}{250} \times 100 = 20\% \quad \text{Ans}$$

2) C.P = Rs.500 , S.P = Rs. 550

**Solution:**

$$\Rightarrow S.P - C.P = 550 - 500 = \text{Rs. } 50$$

$$\text{Profit percentage} = \frac{50}{500} \times 100 = 10\% \quad \text{Ans}$$

3) C.P = Rs.500 , S.P = Rs.450

**Solution:**

$$\Rightarrow S.P - C.P = 500 - 450 = \text{Rs. } 50$$

$$\text{Profit percentage} = \frac{50}{500} \times 100 = 10\% \quad \text{Ans}$$

4) C.P = Rs.1500 , S.P = Rs. 1200

**Solution:**

$$\Rightarrow S.P - C.P = 1500 - 1200 = \text{Rs. } 300$$

$$\text{Loss percentage} = \frac{300}{1500} \times 100 = 20\% \quad \text{Ans}$$

5) C.P = Rs. 400 , S.P = Rs. 390

Solution:

$$\Rightarrow \text{Loss} = \text{C.P} - \text{S.P} = 400 - 390 = \text{Rs. } 10$$

$$\text{Loss percentage} = \frac{10}{400} \times 100 = 2.5\% \quad \text{Ans}$$

6) C.P = Rs. 1150 , S.P = Rs. 1380

Solution:

$$\Rightarrow \text{S.P} - \text{C.P} = 1380 - 1150 = \text{Rs. } 230$$

$$\text{Profit percentage} = \frac{230}{1150} \times 100 = 20\% \quad \text{Ans}$$

7) C.P = Rs. 550 , S.P = Rs. 473

Solution:

$$\Rightarrow \text{S.P} - \text{C.P} = 550 - 473 = \text{Rs. } 77$$

$$\text{Loss percentage} = \frac{77}{550} \times 100 = 14\% \quad \text{Ans}$$

8) If the cost price of a shirt is Rs. 400 and its sale price is Rs. 444, find profit percent.

$$\Rightarrow \text{C. S} = 444 - \text{Rs. } 400 = \text{Rs. } 44$$

$$\frac{44}{400} \times 100 = 11\% \quad \text{Ans}$$

9) If the cost price of a book is Rs. 300 and the selling price is Rs. 270, find loss percent.

Solution:

$$\Rightarrow \text{C. S} = \text{Rs. } 300 - \text{S.P} = \text{Rs. } 270 = \text{Rs. } 30$$

$$\frac{30}{300} \times 100 = 10\% \quad \text{Ans}$$

10) Aziz khan bought 60 pencils at the rate of Rs. 30 per dozen and sold them for Rs.33 per dozen. Find his gain or loss percent.

**Solution:**

$$\Rightarrow 30 / 12 = \text{Rs. } 2.50$$

R. 5.2.50, Rs 150

$$\frac{33}{12} = 2.75$$

Total selling price = 60 pencils = 2.75, pencil = 165.

$$\text{Rs. } 165 - \text{Rs. } 150 = \text{Rs. } 15$$

$$\frac{15}{150} \times 100 = 10\% \quad \text{Ans}$$

**Exercise 4.2**

1) find the selling price an article which was bought for Rs. 325 and sold at the profit of 20%

**Solution:**

$$\Rightarrow 12\% = 0.12 \times 325 = 39$$

$$325 + 39 = 364 \quad \text{Ans}$$

2) Saif bought at ratio for Rs.1900 and sold it at a loss of 50%.find the selling price of the ratio.

**Solution:**

$$\Rightarrow 15\% = 0.15 \times 1900 = 285$$

$$1900 - 285 = 1615 \quad \text{Ans}$$

3) A chair bought for Rs.480 is sold at a profit of 28% find the selling price of chair

**Solution:**

$$\Rightarrow 28\% = 0.28 \times 480 = 134.4$$
$$480 + 134.4 = 614.4 \quad \text{Ans}$$

4) Asif khan was bought a goat for Rs.2300 and sold it to Ali on 10% loss. How much ali spend on the goat?

**Solution:**

$$\Rightarrow 10\% = 0.10 \times 2300 = 230$$
$$2300 - 230 = 2070 \quad \text{Ans}$$

5) A book sells bought 5 dozen of exercise books at Rs.40 per dozen. How should the sell them to gain 10%.

**Solution:**

$$\Rightarrow 5 \times 40 = 200, 10\% = 0.10 \times 200 = 20$$
$$200 + 20 = 220 \quad \text{Ans}$$

6) Find the selling price of house which was purchased for Rs. 100000 and sold at a gain of 10%?

**Solution:**

$$\Rightarrow 10\% = 0.10 \times 100000 = 10000$$
$$100000 + 10000 = 110000 \quad \text{Ans}$$

7) An article is sold for Rs. 720 at a profit of 20% find its cost price.

**Solution:**

$$\Rightarrow 720 = x + 0.20x, \quad 720 = 1.20x$$
$$x = \frac{720}{1.20} = 600 \quad \text{Ans}$$

8) Rahid sold a goat for Rs. 1200 at 20% profit find the cost price of the goat?

**Solution:**

$$\Rightarrow 1200 = x + 0.20x, \quad 1200 = 1.20x$$
$$x = \frac{1200}{1.20} = 600 \quad \text{Ans}$$

9) What is the cost price of an article which when sold for Rs. 400, a loss of 20% occurs?

**Solution:**

$$\Rightarrow 400 = x - 0.20x, \quad 400 = 0.80x$$
$$x = \frac{400}{0.80} = 500 \quad \text{Ans}$$

10) A profit of 10% is made by selling a bicycle for Rs. 600. Find its cost price.

**Solution:**

$$\Rightarrow 1.10 \times CP = 600$$

$$CP = \frac{600}{1.10} = 545.45 \quad \text{Ans}$$

11) A leader made a profit of 30% by selling on article for Rs.104. How much did it cost him?

**Solution:**

$$\Rightarrow 30\% = 1.30, 1.30 \times CP = 104$$

$$CP = \frac{104}{1.30} = 80 \quad \text{Ans}$$

**Exercise 4.3**

1) Find the S.P of the following.  
1) M.P = Rs. 210, Discount = 12%

**Solution:**

$$\Rightarrow S.P = 210 \times \left(1 - \frac{12}{100}\right) = 210 \times 0.88 = 184.8 \quad \text{Ans}$$

2) M.P = Rs. 2010, Discount = 8%

**Solution:**

$$\Rightarrow S.P = 2010 \times \left(1 - \frac{8}{100}\right) = 2010 \times 0.92 = 1849.2 \quad \text{Ans}$$

3) M.P Rs. 15240, Discount = 9%

**Solution:**

$$\Rightarrow S.P = 15240 \times \left(1 - \frac{9}{100}\right) = 15240 \times 0.91 = 13874.4 \quad \text{Ans}$$

4) M.P = Rs. 640, Disount =  $12 \frac{1}{2}\%$

**Solution:**

$$\Rightarrow S.P = 640 \times \left(1 - \frac{25}{200}\right) = 640 \times 0.71 = 480 \quad \text{Ans}$$

2) Find the C.P if.

1) S.P Rs. 270 , Discount = 10%

Solution:

$$\Rightarrow \text{C.P} = \frac{270}{1 - \frac{10}{100}} = \frac{270}{0.9} = 300 \quad \text{Ans}$$

2) S.P Rs. 1275 , Discount = 15%

Solution:

$$\Rightarrow \text{C.P} = \frac{1275}{1 - \frac{15}{100}} = \frac{1275}{0.85} = 1500 \quad \text{Ans}$$

3) SP. Rs. 11340 , Discount =  $5 \frac{1}{2}\%$

Solution:

$$\Rightarrow \text{C.P} = \frac{11340}{1 - \frac{5.5}{100}} = \frac{11340}{0.945} = 12000 \quad \text{Ans}$$

4) S.P Rs. 1275 , Discount = 4%

Solution:

$$\Rightarrow \text{C.P} = \frac{1275}{1 - \frac{4}{100}} = \frac{1275}{0.96} = 1328.125 \quad \text{Ans}$$

3) Find the discount percent if.

1) M.P = Rs. 300, S.P = Rs. 275

Solution:

$$\Rightarrow \text{Discount\%} = \frac{300 - 275}{300} \times 100 = \frac{25}{300} \times 100 = 7\% \quad \text{Ans}$$

2) M.P Rs.760 , SP = Rs.722

**Solution:**

$$\Rightarrow \text{Discount\%} = \frac{760-722}{760} \times 100 = \frac{38}{760} \times 100 = 5\%$$

Ans

3) MP = Rs. 1680, S.P Rs.1512

**Solution:**

$$\Rightarrow \text{Discount\%} = \frac{1680-1512}{1680} \times 100 = \frac{168}{1680} \times 100 = 10\%$$

Ans

4) MP = Rs. 20100 , S.P = Rs.19497

**Solution:**

$$\Rightarrow \text{Discount\%} = \frac{2100-19497}{20100} \times 100 = \frac{603}{20100} \times 100 = 3\%$$

4) A shopkeeper allows 20% discount on an article and still make a profit of 25% if the article cost Rs. 1720 to the shopkeeper, find its maked price.

**Solution:**

$$\text{S.P} = 1720 \times \frac{125}{100} = 2150 \times \frac{80}{100}$$

$$2150 \times \frac{100}{800} = 2687.5 \quad \text{Ans}$$

5) A shopkeeper offers 15% disount on a book E still makes a profit of 10%. What is the cost price of the book if the maked price is Rs.430?

**Solution:**

$$\Rightarrow 15\% = 0.15 \times 430 = \text{Rs.}64.50, 430 - 64.50 = \text{Rs.}365.50 \quad 110\% \times x = 365.50, 1.10x = 365.50$$

$$x = \frac{365.50}{1.10} = \text{Rs.} 332.27 \quad \text{Ans}$$

**Chapter 5****RATIO AND PROPORTION****Exercise 5.1**

1) Find the ratio of the following.

1) 18 meters, 54 meters

**Solution:**

$$\Rightarrow 18 : 54 = \frac{18}{54} = 1 : 3 \quad \text{Ans}$$

2) 16 rupess, 36 rupees

**Solution:**

$$\Rightarrow 16 : 36 = \frac{16}{36} = \frac{4}{9} \quad \text{Ans}$$

3) 247 years, 60 years

**Solution:**

$$\Rightarrow 247 : 60 = \frac{247}{60} = 247 : 60 \text{ Ans}$$

4) 75 kg 35kg

**Solution:**

$$\Rightarrow 75 : 35 = \frac{75}{35} = 15 : 07 \quad \text{Ans}$$

5) 33km 77km

**Solution:**

$$\Rightarrow 33 : 77 = \frac{33}{77} = \frac{3}{7} \quad \text{Ans}$$

6) 126ml , 250 ml

**Solution:**

$$\Rightarrow 126 : 250 = \frac{126}{250} = \frac{1}{2} \quad \text{Ans}$$

7) 400 grams, 600 grams.

**Solution:**

$$\Rightarrow 400 : 600 = \frac{400}{600} = 2 : 3 \quad \text{Ans}$$

8) 850 , 900cm.

**Solution:**

$$\Rightarrow 850 : 900 = \frac{850}{900} = 17 : 18 \quad \text{Ans}$$

9) 1050 liters , 1250 liters

**Solution:**

$$\Rightarrow 1050 : 1250 = \frac{1050}{1250} = 21 : 25 \quad \text{Ans}$$

10) 625 sec , 425sec

**Solution:**

$$\Rightarrow 625 : 425 = \frac{625}{425} = 25 : 17 \text{ Ans}$$

2) Express the following ratios in the simplified form.

1) 55 sec ,  $2\frac{1}{2}$  minutes.

**Solution:**

$$\Rightarrow \frac{55}{5} : \frac{150}{5} = 11 : 30 \quad \text{Ans}$$

2) 2 meter , 75cm

**Solution:**

$$\Rightarrow \frac{200}{25} : \frac{75}{25} = 8 : 3 \quad \text{Ans}$$

3) 2 meter , 75cm

Solution:

$$\Rightarrow \frac{200}{25} : \frac{75}{25} = 8 : 3 \quad \text{Ans}$$

4) 9 inches , 3 feet

Solution:

$$\Rightarrow \frac{9}{9} : \frac{36}{9} = 1 : 4 \quad \text{Ans}$$

5) 1.5 liters , 900 ml

Solution:

$$\Rightarrow \frac{1500}{300} : \frac{900}{300} = 5 : 3 \quad \text{Ans}$$

6) 11 months , 2 years 9 months

Solution:

$$\Rightarrow \frac{11}{11} : \frac{33}{11} = 1 : 3 \quad \text{Ans}$$

7) 75 paisa, 2 rupees , 25 paisa

Solution:

$$\Rightarrow \frac{75}{75} : \frac{225}{75} = 1 : 3 \quad \text{Ans}$$

8) 900 meters , 3 km 600

Solution:

$$\Rightarrow \frac{900}{900} : \frac{3600}{900} = 1 : 4 \quad \text{Ans}$$

9) 750 mg , 3 grams

Solution:

$$\Rightarrow \frac{750}{750} : \frac{3000}{750} = 1 : 4 \quad \text{Ans}$$

10) 65 mm , 13 cm

**Solution:**

$$\Rightarrow 10 \text{ mm} : 130 \text{ mm}, 65 : 130 \quad \text{Ans}$$

**Exercise 5.2**

1) In a playground there are 22 players and 440 spectators. What is the ratio of the number of players to the number of spectators.

**Solution:**

$$\Rightarrow \frac{22}{440}, \frac{22 \div 22}{440 \div 22} = \frac{1}{20} \quad 1 : 20 \quad \text{Ans}$$

2) There are 4900 pages in Mathematics book and 553 pages in urdu book. What is the ratio of the number of pages of Mathematics book to the number of pages of urdu book?

**Solution:**

$$\Rightarrow \frac{4900}{553} = 4900 : 553 \quad \text{Ans}$$

3) An aeroplane covered a distane of 750 km. in 2 hours and a train covered a distance of 225 km in 3 hours. Find the ratio between speeds of the aeroplane and train.

**Solution:**

$$\Rightarrow \frac{750}{2} = 375 \text{ km/ hours}$$

$$\frac{225}{3} = 75 \text{ km / hours}$$

$$\frac{375}{75} = 5 : 1 \quad \text{Ans}$$

4) Aeroplane can carry 366 passengers. A ship can carry 852 passengers. Find the ratio of passengers of the aeroplane to that of the passengers or degrees?

**Solution:**

$$\Rightarrow \frac{366}{852}, \frac{366 \div 6}{852 \div 6} = \frac{61}{142} \text{ Ans}$$

1) Find  $x : y : z$  when:

**Solution:**

$$\begin{array}{rccccc}
 x & : & y & : & z \\
 3 & : & 4 & : & 6 \\
 & & 5 & : & 6 \\
 \hline
 3 \times 5 & 4 \times 5 & 4 \times 6 \\
 15 & 20 & 24 & \text{Ans}
 \end{array}$$

2)  $x : y = 6 : 9$  and  $y : z = 7 : 8$

**Solution:**

$$\begin{array}{rccccc}
 x & : & y & : & z \\
 6 & : & 9 & & \\
 & & 7 & : & 8 \\
 \hline
 6 \times 9 & 9 \times 7 & 7 \times 8 \\
 14 & 21 & 24 & \text{Ans}
 \end{array}$$

3)  $x : y = 4 : 5$  and  $y : z = 3 : 8$

**Solution:**

$$\begin{array}{rccccc}
 x & : & y & : & z \\
 4 & : & 5 & & \\
 & & 3 & : & 8 \\
 \hline
 4 \times 5 & 3 \times 5 & 3 \times 8 \\
 20 & 15 & 24 & \text{Ans}
 \end{array}$$

4)  $x : y = 7 : 10$  and  $y : z = 2 : 5$

**Solution:**

$$\begin{array}{rccccc}
 x & : & y & : & z \\
 7 & : & 10 & & \\
 & & 2 & : & 5 \\
 \hline
 7 \times 10 & & 10 \times 2 & & 2 \times 5 \\
 70 & & 20 & & 10 & \text{Ans}
 \end{array}$$

5)  $x : y = 12 : 4$  and  $y : z = 8 : 13$

**Solution:**

$$\begin{array}{rccccc}
 x & : & y & : & z \\
 12 & : & 4 & & \\
 & & 8 & : & 13 \\
 \hline
 12 \times 4 & & 4 \times 8 & & 8 \times 13 & \text{Ans}
 \end{array}$$

6)  $x : y = 14 : 17$  and  $y : z = 4 : 7$

**Solution:**

$$\begin{array}{rccccc}
 x & : & y & : & z \\
 14 & : & 17 & & \\
 & & 4 & : & 7 \\
 \hline
 14 \times 17 & & 17 \times 4 & & 4 \times 7 & \text{Ans}
 \end{array}$$

2) Find  $a : b : c : d$  when:

1)  $a : b : 2 : 3$ ,  $b : c = 3 : 4$ ,  $c : d = 6 : 7$

**Solution:**

$$\begin{array}{rccccc}
 a & : & b & : & c & : & d \\
 2 & : & 3 & & \\
 & & 3 & : & 4 & & \\
 & & & & 6 & : & 7 \\
 \hline
 2 \times 3 & : & 3 \times 3 & : & 3 \times 4 & & \\
 6 & : & 9 & : & 12 & & 
 \end{array}$$

Or  $\begin{array}{rcl} a & : & b \\ 6 & : & 9 \\ \hline & & 6 \end{array} \quad \begin{array}{rcl} c & : & d \\ 12 & : & 7 \\ \hline & & 7 \end{array}$

$\begin{array}{rcl} 6 \times 6 & : & 9 \times 6 \\ 36 & : & 54 \\ \hline & & 72 \end{array} \quad \begin{array}{rcl} 12 \times 6 & : & 12 \times 7 \\ 72 & : & 84 \\ \hline & & 84 \end{array}$

Divided by 6

$\begin{array}{rcl} 36 \div 6 & : & 54 \div 6 \\ 6 & : & 9 \\ \hline & & 12 \end{array} \quad \begin{array}{rcl} 72 \div 6 & : & 84 \div 6 \\ 12 & : & 14 \\ \hline & & 14 \end{array}$

Answer.

2)  $a : b = 3 : 4$  ,  $b : c = 7 : 8$  ,  $c : d = 5 : 6$

Solution:

$\begin{array}{rcl} a & : & b & : & c \\ 3 & : & 4 & & \\ \hline & & 7 & : & 8 \end{array}$

$\begin{array}{rcl} 3 \times 7 & : & 4 \times 7 & : & 4 \times 8 \\ 21 & : & 28 & : & 32 \\ \hline & & & & \end{array}$

Or  $\begin{array}{rcl} a & : & b & : & c & : & d \\ 21 & : & 28 & : & 32 & & \\ \hline & & & & 5 & : & 6 \end{array}$

$\begin{array}{rcl} 21 \times 5 & : & 28 \times 5 & : & 32 \times 5 & : & 32 \times 6 \\ 105 & : & 140 & : & 160 & : & 192 \\ \hline & & & & & & \end{array}$

Answer.

3)  $a : b = 5 : 9$  ,  $b : c = 7 : 8$  ,  $c : d = 5 : 6$

Solution:

$\begin{array}{rcl} a & : & b & : & c \\ 5 & : & 9 & & \\ \hline & & 7 & : & 8 \end{array}$

$\begin{array}{rcl} 5 \times 7 & : & 9 \times 7 & : & 9 \times 8 \\ 35 & : & 63 & : & 72 \\ \hline & & & & \end{array}$

Or  $\begin{array}{rcl} a & : & b & : & c & : & d \\ 35 & : & 63 & : & 72 & & \\ \hline & & & & 5 & : & 6 \end{array}$

$$\begin{array}{rccccc}
 35 & : & 63 & : & 72 & : \\
 & & & 5 & : & 6 \\
 \hline
 35 \times 5 & : & 63 \times 5 & : & 72 \times 5 & : & 72 \times 6 \\
 175 & : & 315 & : & 360 & : & 432
 \end{array}$$

Answer

4)  $a:b = 7:10$ ,  $b:c = 8:11$ ,  $c:d = 9:13$

Solution:

$$\begin{array}{rccccc}
 a & : & b & : & c \\
 7 & : & 10 & & \\
 \hline
 & 8 & : & 11 & \\
 7 \times 8 & : & 10 \times 8 & : & 10 \times 11 \\
 56 & : & 80 & : & 110 \\
 \text{Or} & a & : & b & : & c & : & d \\
 56 & : & 80 & : & 110 & : & \\
 & & & & 9 & : & 13 \\
 \hline
 56 \times 9 & : & 80 \times 9 & : & 110 \times 9 & : & 10 \times 13 \\
 504 & : & 720 & : & 990 & : & 130
 \end{array}$$

Answer

5)  $a:b = 8:13$ ,  $b:c = 4:7$ ,  $c:d = 6:11$

Solution:

$$\begin{array}{rccccc}
 a & : & b & : & c \\
 8 & : & 13 & & \\
 \hline
 & 4 & : & 7 & \\
 8 \times 4 & : & 13 \times 4 & : & 13 \times 7 \\
 32 & : & 52 & : & 91 \\
 \text{Or} & a & : & b & : & c & : & d \\
 32 & : & 52 & : & 91 & : & \\
 & & & & 6 & : & 11 \\
 \hline
 32 \times 6 & : & 52 \times 6 & : & 91 \times 6 & : & 91 \times 11
 \end{array}$$

$$192 : 312 : 546 : 1001$$

Answer

3) fahim has some marbles of green , yellow, blue and red colours. The ratio blw the number green e yellow marbles in  $3 : 4$ , yellow and blue is  $5 : 7$  and blue and red is  $8 : 9$ , what is the ratio blw the numbers of green and blue marbles.

**Solution:**

$$\begin{array}{rcccl}
 \text{Green} & : & \text{Yellow} & : & \text{Blue} \\
 3 & : & 4 & & \\
 & & 5 & : & 7 \\
 \hline
 3 \times 4 & : & 4 \times 5 & : & 4 \times 7 \\
 15 & : & 20 & : & 28
 \end{array}$$

Or green : yellow : blue : red

$$\begin{array}{rcccl}
 15 & : & 20 & : & 28 \\
 & & 8 & : & 9 \\
 \hline
 15 \times 8 & : & 20 \times 8 & : & 28 \times 8 & : 28 \times 9 \\
 120 & : & 160 & : & 224 & : 252
 \end{array}$$

$$\begin{array}{rcccl}
 \text{Or} & 20 \div 8 & : & 160 \div 8 & : 224 \div 8 : 252 \div 8 \\
 & 15 & : & 20 & : 28 & : 31.5
 \end{array}$$

$$\text{Green} = 215$$

$$\text{Blue} = 28 \quad \text{Answer.}$$

4) Of the runs blw 1<sup>st</sup> and 2<sup>nd</sup> tests matches is 9 is to 13. Blw 2<sup>nd</sup> and 3<sup>rd</sup> tests matches is 7 is to 8. Find the ratio of the runs blw 1<sup>st</sup> and the 4<sup>th</sup> test matches.

**Solution:**

$$\begin{array}{ccccccc}
 1^{\text{st}} & : & 2^{\text{nd}} & : & 3^{\text{rd}} \\
 9 & : & 13 & & \\
 & & 5 & : & 3 \\
 \hline
 9 \times 5 & : & 13 \times 5 & : & 13 \times 3 \\
 45 & : & 65 & : & 39 \\
 \text{Or} \quad 1^{\text{st}} & : & 2^{\text{nd}} & : & 3^{\text{rd}} & : & 4^{\text{th}} \\
 45 & : & 65 & : & 39 & & \\
 & & & & & 7 & : 8 \\
 \hline
 45 \times 7 & : & 65 \times 7 & : & 39 \times 7 & : & 39 \times 8 \\
 315 & : & 455 & : & 273 & : & 312 \\
 \text{Or} \quad 315 \div 8 & : & 455 \div 7 & : & 273 \div 7 & : & 312 \div 7 \\
 45 & : & 65 & : & 39 & : & 45 \\
 1^{\text{st}} = 45 \text{ and } 4^{\text{th}} = 45 & & \text{Answer.} & & & & 
 \end{array}$$

**Exercise 5.4**

1) Which of the following expressions are in proportion.  
 1)  $7 : 21 :: 3 : 9$

**Solution:**

$$\Rightarrow \frac{7}{21} = \frac{1}{3} \text{ and } \frac{3}{9} = \frac{1}{3} \text{ Proportion} \quad \text{Ans}$$

$$2) \quad 2 : 5 :: 4 : 3$$

**Solution:**

$$\Rightarrow \frac{2}{5} = 0.4 \text{ and } \frac{4}{3} \approx 1.33 \text{ not Proportion} \quad \text{Ans.}$$

$$3) \quad 3 : 1 :: 48 : 15$$

**Solution:**

$$\Rightarrow \frac{3}{1} = 3 \text{ and } \frac{48}{15} = \frac{16}{5} = 3.2 \text{ not proportion} \quad \text{Ans.}$$

4)  $2 : 4 :: 8 : 16$

**Solution:**

$$\Rightarrow \frac{2}{4} = \frac{1}{2} \text{ and } \frac{8}{16} = \frac{1}{2} \quad \text{Proportion} \quad \text{Ans.}$$

5)  $6 : 1 :: 12 : 14$

**Solution:**

$$\Rightarrow \frac{6}{1} = 6 \text{ and } \frac{12}{14} = \frac{6}{7} \approx 0.8 \text{ not Proportion} \quad \text{Ans.}$$

6)  $6 : 8 :: 4 : 5$

**Solution:**

$$\Rightarrow \frac{6}{8} = \frac{3}{4} = 0.75 \text{ and } \frac{4}{5} \approx 0.8 \text{ not Proportion} \quad \text{Ans.}$$

7)  $5 : 8 :: 20 : 32$

**Solution:**

$$\Rightarrow \frac{5}{8} = 0.625 \text{ and } \frac{20}{32} = \frac{5}{8} = 0.625 \text{ Proportion} \quad \text{Ans.}$$

8)  $8 : 7 :: 6 : 9$

**Solution:**

$$\Rightarrow \frac{8}{7} \approx 1.14 \text{ and } \frac{6}{9} = \frac{2}{3} \approx 0.67 \text{ not proportion} \quad \text{Ans.}$$

9)  $13 : 4 :: 5 : 9$

**Solution:**

$$\Rightarrow \frac{13}{4} = 3.25 \text{ and } \frac{5}{9} \approx 0.56 \text{ not proportion} \quad \text{Ans.}$$

10)  $16 : 32 :: 1 : 2$

**Solution:**

$$\Rightarrow \frac{16}{32} = \frac{1}{2} \text{ and } \frac{1}{2} = \frac{1}{2} \quad \text{proportion} \quad \text{Ans.}$$

11)  $200 : 100 :: 400 : 200$

**Solution:**

$$\Rightarrow \frac{200}{100} = 2 \text{ and } \frac{400}{200} = 2 \quad \text{proportion} \quad \text{Ans.}$$

12)  $31 : 6 :: 124 : 24$

**Solution:**

$$\Rightarrow \frac{31}{6} \approx 5.17 \text{ and } \frac{124}{24} = \frac{31}{6} \approx 5.17 \text{ proportion} \quad \text{Ans.}$$

2) Find the value of the  $x$  in the following proportion.

1)  $3 : 7 :: 15\% x$

**Solution:**

$$3 \times x = 7 \times 15 \\ 3x = 105, x = \frac{105}{3}, x = 35 \quad \text{Ans.}$$

2)  $15 : 9 :: 10 : x$

**Solution:**

$$\Rightarrow 15 \times x = 9 \times 10 \\ 15x = 90 \\ x = \frac{90}{15} = x 6 \quad \text{Ans.}$$

3)  $6 : 4 :: 12 : x$

**Solution:**

$$\Rightarrow 6 \times x = 4 \times 12$$

$$6x = 48$$
$$x = \frac{48}{6} = x 8$$

Ans.

4)  $8 : 12 :: x : 15$

**Solution:**

$$\Rightarrow 8 \times 15 = 12 \times x$$
$$120 = 12x$$
$$\frac{120}{12} = x = 10$$

Ans.

5)  $6 : 8 :: x : 4$

**Solution:**

$$\Rightarrow 6 \times 4 = 8 \times x$$
$$24 = 8x$$
$$\frac{24}{8} = x = 3$$

Ans.

6)  $11 : 5 :: x : 20$

**Solution:**

$$\Rightarrow 11 \times 20 = 5 \times x$$
$$220 = 5x$$
$$\frac{220}{5} = x = 44$$

Ans.

7)  $7 : x :: 14 : 8$

**Solution:**

$$\Rightarrow 7 \times 8 = x \times 14$$

$$56 = 14 x$$

$$\frac{56}{14} = x = 4$$

Ans.

$$8) \quad 9 : x :: 18 : 36$$

Solution:

$$\Rightarrow 324 = 18 x$$

$$\frac{324}{18} = x = 18$$

Ans.

$$9) \quad x : 4 :: 10 : 8$$

Solution:

$$\Rightarrow x \times 8 = 4 \times 10$$

$$8 x = 40$$

$$x = \frac{40}{8} = x = 5$$

Ans.

$$10) \quad x : 16 :: 7 : 8$$

Solution:

$$\Rightarrow x \times 8 = 16 \times 7$$

$$8 x = 112$$

$$x = \frac{112}{8} = x = 14$$

Ans.

$$11) \quad x : 25 :: 3 : 15$$

Solution:

$$\Rightarrow x \times 15 = 75$$

$$x = \frac{75}{15} = x = 5$$

Ans.

3) The price of 9 pens is Rs. 90. Find the price of 20 such pens.

**Solution:**

$$\Rightarrow \frac{90}{9} = 10 \text{ Rs}$$
$$20 \times 10 = 200 \text{ Rs}$$

Ans.

4) The distance of 27 km is represented by 3 cm on a map. How many centimete's long line segment will represent 90 km long road?

**Solution:**

$$\Rightarrow \frac{27}{3} = \frac{90}{x}$$
$$27x = 270$$
$$x \frac{270}{27} = 10$$

Ans.

5) An aeroplane covers a distance of 720 kilometers in 4 hours. How much distance would cover in 6 hours?

**Solution:**

$$\Rightarrow \frac{720}{4} = 180$$
$$180 \times 6 = 1080 \text{ km}$$

Ans

6) kishwa buys 2 dozen oranges for Rs. 36. How many dozen orange would she buy for Rs. 108?

**Solution:**

$$\Rightarrow \frac{36}{2} = 18 \text{ Rs.}$$

$$108 = \frac{108}{18} = 6 \quad \text{Ans.}$$

7) 9 men earn Rs: 360. How many men earn Rs: 1000?

**Solution:**

$$\Rightarrow \frac{360}{9} = 40 \text{ Rs.}$$

$$\frac{1000}{40} = 25 \text{ mens} \quad \text{Ans.}$$

8) 400 men had a food stock for 6 days. How many men would eat the same stock of food in 8 days?

**Solution:**

$$6 : 8 :: 400 : x$$

$$6x = 3200$$

$$x = \frac{3200}{6} = x = 533.3 \quad \text{Ans.}$$

9) 30 men can do a piece of work in 18 days. If how many days the same work would complete 15 mens?

**Solution:**

$$\begin{array}{ll} \text{mens} & \text{days} \\ 30 & 18 \\ 15 & x \end{array}$$

$$30 : 15 :: 18 : x$$

$$x = \frac{15 \times 18}{30} = \frac{270}{30}$$

$$x = 9 \text{ days} \quad \text{Ans.}$$

10) In a camp 450 men had food for 33 days? If 100 more men arrived, find for how many days would the food be sufficient?

**Solution:**

Mens	days
450	33
100	x
450 : 100 :: x : 33	

$$x = \frac{450 \times 33}{100} = \frac{14850}{100}$$

$$450 \text{ mens} + 100 \text{ men} = 55 \text{ over}$$

$$x = \frac{1480 - 33}{550} = 27 \text{ days.}$$

---

## Chapter 6

### ALGEBRAIC EXPRESSIONS, FUNDAMENTAL OPERATION AND LINEAR EQUATION

#### Exercise 6.1

a) Find the sum of the following algebraic expressions:

1)  $6x + 4x$       2)  $8xy + 9x y$

Solution:

$\Rightarrow 10x$       Ans       $\Rightarrow 17xy$       Ans

3)  $a^2b + 18a^2b$       4)  $7a + 3a + 9a$

Solution:

$\Rightarrow 19a^2b$       Ans       $\Rightarrow 19a$       Ans

5)  $a^2c + 8a^2c$

Solution:

$\Rightarrow 18a^2c$

6)  $2ab^2c + 6ab^2c + 11ab^2c$

Solution:

$\Rightarrow 19ab^2c$

Ans

Ans

7)  $\frac{2}{5}a^2 + \frac{6}{5}a^2$

Solution:

$\Rightarrow \frac{8}{5}a^2$       Ans

8)  $\frac{1}{4}ab + \frac{8}{4}ab$

Solution:

$\Rightarrow \frac{9}{4}ab$       Ans

9)  $\frac{3}{5}y^2 + \frac{8}{15}y^2 + \frac{6}{5}y^2$

**Solution:**

$$\Rightarrow \frac{7}{3} y^2 \quad \text{Ans}$$

$$10) \quad \frac{9}{4} abc + \frac{2}{3} abc + \frac{5}{12} abc$$

**Solution:**

$$\Rightarrow \frac{55}{36} abc \quad \text{Ans}$$

b) Find the difference of the following algebraic expressions:

$$1) \quad 6x - 4x$$

$$2) \quad 8a - a$$

**Solution:**

$$\Rightarrow 2x$$

Ans

$$\Rightarrow 7a$$

Ans

$$3) \quad 17a^2 - 16a^2$$

$$4) \quad 9x^3y^2 - 3x^3y^2$$

**Solution:**

$$\Rightarrow a^2$$

Ans

$$\Rightarrow 6x^3y^2$$

Ans

$$5) \quad 10xy^2 - 9xy^2$$

$$6) \quad 21abc - 19abc$$

**Solution:**

$$\Rightarrow xy^2$$

Ans

$$\Rightarrow 2abc$$

Ans

$$7) \quad 14x^2y^2 - 9x^2z^2$$

$$8) \quad \frac{8}{5}a \cdot \frac{2}{5}a$$

**Solution:**

$$\Rightarrow 5x^2yz^2$$

Ans

$$\Rightarrow \frac{6}{5}a$$

Ans

9)  $\frac{9}{15} x^2 - \frac{2}{5} x^2$

Solution:

$\Rightarrow \frac{1}{5} x^2$  Ans

10)  $xy - \frac{3}{4} xy^2$

Solution:

$\Rightarrow \frac{1}{4} xy^2$  Ans

c) Simplify the following algebraic expression:

1)  $7p + 3p - 4p$

Solution:

$\Rightarrow 6p$  Ans

2)  $3y^2 - 9y^2 + 12y^2$

Solution:

$\Rightarrow 6y^2$  Ans

3)  $2x^2 - 11x^2 + 15x^2$

Solution:

$\Rightarrow 6x^2$  Ans

4)  $3a - 7a - 8a + 3a - 2a$

Solution:

$\Rightarrow 3a$  Ans

5)  $y^2 + y^2 + y^2 + y^2$

Solution:

$\Rightarrow 4y^2$  Ans

6)  $\frac{5}{3} x + \frac{4}{9} x + \frac{5}{3} x$

Solution:

$\Rightarrow \frac{34}{9} x$  Ans

7)  $\frac{17}{6} a - \frac{1}{2} a + \frac{1}{6} a$

Solution:

$\Rightarrow \frac{5}{2} a$  Ans

8)  $20 xyz - 10 xyz + 5xyz$

Solution:

$\Rightarrow 15 xyz$  Ans

9)  $2a^2 b^2 c^2 - 5 a^2 b^2 c^2 + 9 a^2 b^2 c^2 - 8 c^2 b^2 c^2$

Solution:

$\Rightarrow -2a^2 b^2 c^2$  Ans

**Exercise 6.2**

1) Arrange the following algebraic expression in descending and ascending orders with respect to the given variable in each expression.

1)  $a^2 + 4a^3 - 3a + 4 + 3a^2$

**Solution:**

$$\Rightarrow 4a^3 + 3a^2 + a^2 + 3a + 4$$

Descending order

$$\Rightarrow 4 + 3a + a^2 + 3a^2 + 4a^3$$

Ascending order

Ans.

2)  $4x^6 - 8 + 3x + 7x^2 + 8x^3$

**Solution:**

$$\Rightarrow 4x^6 + 8x^3 + 7x^2 + 3x - 8$$

Descending order

$$\Rightarrow -8 + 3x + 7x^2 + 8x^3 + 4x^6$$

Ascending order

Ans.

3)  $5 - x + 4x^4 - 2x^3 + 3x^2$

**Solution:**

$$\Rightarrow 4x^4 - 2x^3 + 3x^2 - x + 5$$

Descending order

$$\Rightarrow 5 - x + 3x^2 - 2x^3 + 4x^4$$

Ascending order

Ans.

4)  $y^7 + 4y^6 - 10 + 3y^5 + 4y^2$

**Solution:**

$$\Rightarrow 4y^7 + 4y^6 + 3y^5 + 4y^2$$

Descending order

$$\Rightarrow -10 + 4y^2 + 3y^5 + 4y^6 + y^7$$

Ascending order

Ans.

5)  $3z^2 + z + 4z^3 - 6z^4$

**Solution:**

$$\Rightarrow -6z^4 + 4z^3 + 3z^2 + z$$

Descending order

$$\Rightarrow z + 3z^2 + 4z^3 - 6z^4$$

Ascending order

Ans.

6)  $2b^2 - 6b^3 + 7b - 12 + 6b^4$

**Solution:**

$$\Rightarrow 6b^4 - 6b^3 + 2b^2 + 7b - 12$$

Descending order

$$\Rightarrow -12 + 7b + 2b^2 - 6b^3 + 6b^4$$

Ascending order

Ans.

7)  $C^3 - C^5 + 2C^6 - 4C - 3C^4 + 5C^2$

**Solution:**

$$\Rightarrow 2C^6 - C^5 - 3C^4 + C^3 + 5C^2 - 4C$$

Descending order

$$\Rightarrow -4C + 5C^2 + C^3 - 3C^4 - C^5 + 2C^6$$

Ascending order

Ans.

8)  $2p - 7p^4 + 8 - p^6 + 6p^3$

**Solution:**

$$\Rightarrow -p^6 - 7p^4 + 6p^3 + 2p^4 + 8$$

Descending order

$$\Rightarrow 8 + 2p + 6p^5 - 7p^4 - p^6$$

Ascending order

Ans.

9)  $q^6 + q^3 + 2q^7 + 4q^2 - 8q$

**Solution:**

$$\Rightarrow 2q^7 + q^6 + q^3 + 2q^2 - 8q$$

Descending order

$$\Rightarrow 8q + 4q^2 + q^3 + q^6 + 2q^7$$

Ascending order

Ans.

10)  $x - x^5 + x^2 + 7x^3 + 6 + x^6$

**Solution:**

$$\Rightarrow x^6 - x^5 + 7x^3 + x^2 + x + 6$$

Descending order

$$\Rightarrow 6 + x + x^2 + 7x^3 - x^5 + x^6$$

Ascending order

Ans.

2) Arrange the following in descending and ascending orders with respect to variable 'x'.

1)  $4x^2y - 3x^5y + 6x^3y^4z + 8xy^5$

**Solution:**

$$\Rightarrow -3x^5y + 6x^3y^4z + 4x^2y + 8xy^5$$

Descending order

$$\Rightarrow 8xy^5 + 4x^2y + 6x^3y^4z - 3x^5y^2$$

Ascending order

Ans.

2)  $7xy^3z^4 + 2x^5y^2z - 4x^3y^7z^5 + 4x^4y^4z^4$

**Solution:**

$$\Rightarrow 2x^5y^2z - 4x^4y^4z^4 - 4x^3y^7z^5 + 7xy^3z^4$$

Descending order

$$\Rightarrow 7xy^3z^4 - 4x^3y^7z^5 + 4x^4y^4z^4 + 7xy^3z^4$$

Ascending order

Ans.

3)  $x^3 y^2 z^2 - 6 x^6 y^7 z^5 + 2 x^5 y^3 - 4 x^4 y z^4 + 2 x^2 y^4 z^2$

Solution:

$$\Rightarrow -6 x^6 y^7 z^5 + 2 x^3 y^3 - 4 x^4 y z^4 + x^3 y^2 z^2$$

Descending order

$$\Rightarrow 2x^2 y^2 z^2 + x^3 y^2 z^2 - 4 x^4 y z^4 + 2 x^3 y^3 - 6 x^6 y^7 z^5$$

Ascending order Ans.

4)  $x^4 y^7 + 3x y^6 + 2x^2 y z + 4x^3 y^2 z^2 + 5x^5 y^4 z$

Solution:

$$\Rightarrow 5x^5 y^4 z + x^4 y^7 + 4 x^3 y^2 z^2 + 2 x^2 y z + 3x y^6$$

Descending order

$$\Rightarrow 3 x y^6 + 2x^2 y z + 4x^3 y^2 z^2 + x^4 y^7 + 5x^5 y^4 z$$

Ascending order Ans.

5)  $21 x^6 y^3 z^4 - 7x^7 y z + 3x^2 y^2 z^3 + 7x^3 y - x^4 y^4$

Solution:

$$\Rightarrow 7x y z + 21 x^6 y^3 z^4 + 7x^3 y + 3x^2 y^2 z^3$$

Descending order

$$\Rightarrow 3x^2 y^2 + 7 x^3 y - x^4 y^4 + 21 x^6 y^3 z^4 - 7x^7 y z$$

Ascending order Ans.

6)  $3 x^4 y^2 + 4 x^3 y^3 + 8 x y x^4 + 9 x^5 y^6$

Solution:

$$\Rightarrow 9 x^5 y^6 + 3 x^4 y^2 + 4 x^2 y^3 + 8 x y^4$$

Descending order

$$\Rightarrow 8 x y^4 + 4 x^2 y^3 + 3 x^4 y^2 + 9 x^5 y^6$$

Ascending order Ans

$$7) \quad 10x^7y^2z^2 + 2x^4y^2z^2 + 8x^3y^5z^3 + 3x^5y^3z^2$$

### Solution:

$$\Rightarrow 3x^5y^3z^2 + 2x^4y^2z^5 + 8x^3y^5z^3 - 10x^2y^7z^2$$

Descending order

$$8) \quad 2x^3y^2z^4 - 3x^5yz^2 + 5x^2y^3 + 7x^4y^4$$

### Solution:

$$\Rightarrow \quad -3x^5yz^2 + 7x^4y^4 + 2x^3y^2z^4 + 5x^2y^3$$

Descending order

### Exercise 6.3

1) Add the following algebraic expression:

$$1) \quad x, x \quad 2) \quad x, 2x, 3x$$

### Solution:

### Solution:

$$\Rightarrow 2x \text{ Ans.}$$

$$\Rightarrow 6x \quad \text{Ans.}$$

$$3) \quad 3x^2, 4x^2 2 x^2$$

### Solution:

$$\Rightarrow 9x^2 \text{ Ans.}$$

$$4) \quad 5a^2, 7a^2$$

### Solution:

$$\Rightarrow 12a \quad \text{Ans.}$$

$$5) \quad 8xy - 3xy, 5x y$$

### Solution:

$$\Rightarrow 10yx \text{ Ans.}$$

$$6) \ 6x y^2, -4x y^2 - xy^2$$

### Solution:

$$\Rightarrow x y^2 \quad \text{Ans.}$$

7)  $\frac{3}{4}ab, \frac{5}{4}ab$

**Solution:**

$\Rightarrow 2ab$  Ans.

8)  $14b^2, -7b^2, 8b^2$

**Solution:**

$\Rightarrow 15b^2$  Ans.

9)  $2abc, -abc, -9abc$

**Solution:**

$\Rightarrow -8abc$  Ans.

10)  $\frac{1}{7}x^2y^2, \frac{4}{7}x^2y^2, \frac{2}{7}x^2y^2$

**Solution:**

$\Rightarrow x^2y^2$  Ans.

2) Find the sum of the following vertical method.

1)  $10a^2 + 5b^2 - 8c^2 - 7a^2 - 2b^2 - 4c^2$

**Solution:**

$\Rightarrow 17a^2 + 3b^2 - 12c^2$  Ans.

2)  $4x^2 + 2x^2 + 3x, 5x^3 - 2x^2 - 8x, 6x^3 + 5x^2 + 10x$

**Solution:**

$\Rightarrow 3x^3 + 5x^2 + 5x$

3)  $4p^2 + 3pq + 5q^2, 7p - 6pq - 2q^2, -3p^2 + 2pq - 3q^2$

**Solution:**

$\Rightarrow sp^2 + 6pq$  Ans.

4)  $30x - 4ab + 6c^2, 9ax, 8ab + 14c^2, -11ax, 5ab, 7c^2$

**Solution:**

$\Rightarrow a x - ab + 13c^2$  Ans.

5)  $a + b - 3b^2 + c^2$ ,  $a - 2b^2 - c^2$ ,  $2a + 4b^2 + c^2$

**Solution:**

$$\Rightarrow 4a + 5b^2 + c^2 \quad \text{Ans.}$$

6)  $2x^4 y^2 + 3z^2 - z$ ,  $4x^4 y^2 + 6x^2 - 4z$ ,  $5x^4 y^2 + 7z^2 + 5z$

**Solution:**

$$\Rightarrow 11x^4 y^2 + 16z^2 \quad \text{Ans.}$$

7)  $\frac{1}{2} a^2 b^2 + \frac{3}{4} c^2$ ,  $\frac{3}{2} a^2 b^2 - \frac{7}{4} c^2$

**Solution:**

$$\Rightarrow 2a^2 b^2 - c^2 \quad \text{Ans.}$$

8)  $6a^2 b^2 - 2c^2 - 8d$ ,  $4a^2 b^2 + 4c^2 + 4d$

**Solution:**

$$\Rightarrow 10a^2 b^2 + 2c^2 - 4d \quad \text{Ans.}$$

9)  $8p^2 + 7q^2 - 6pq$ ,  $-7p^2 - 6q^2 + 5pq$

**Solution:**

$$\Rightarrow p^2 + q^2 - pq \quad \text{Ans.}$$

10)  $a^2 + b^2 + c^3$ ,  $-4a^3$ ,  $5b^3$ ,  $10c^3$

**Solution:**

$$\Rightarrow 3a^2 + 6b^3 + 11c^2 \quad \text{Ans.}$$

**Exercise 6.4**

Substract:

1)  $7x$  from  $10x$

2)  $+8a^2$  from  $+15a^2$

**Soltuion:**

$$\Rightarrow 3x \quad \text{Ans.}$$

**Solution:**

$$\Rightarrow 7a^2 \quad \text{Ans.}$$

3)  $-10y^2$  from  $+20y^2$

4)  $-9x y$  from  $-18x y^2$

**Soltuion:**

$$\Rightarrow 30y^2 \quad \text{Ans.}$$

**Solution:**

$$\Rightarrow -9x y \quad \text{Ans.}$$

5)  $+20x^2y^2$  from  $+25x^2y^2$

**Soltuion:**

$$\Rightarrow 45x^2y^2 \quad \text{Ans.}$$

6)  $3a^2 + b^2$  from  $3a^2 + 7b^2$

**Solution:**

$$\Rightarrow 6b^2 \quad \text{Ans.}$$

7)  $7x^2 - 10y^2$  from  $9x^2 + 17y^2$

**Solution:**

$$\Rightarrow 2x^2 + 27y^2 \quad \text{Ans.}$$

8)  $6x - 5y + 4z$  from  $9x - 2y + 6z$

**Solution:**

$$\Rightarrow 4a^2 + 13b^2 - 3c^2 + 3 \quad \text{Ans.}$$

9)  $3a^2 - 4b^2 - 3c^2 + 4$  from  $7a^2 + 9b^2 - 6c^2 + 7$

**Solution:**

$$\Rightarrow 4a^2 + 13b^2 - 3c^2 + 3 \quad \text{Ans.}$$

10)  $-y^3 + y^2 + 3y + 6$  from  $y^3 - 7y^2 + 5y + 8$

**Solution:**

$$\Rightarrow -2y^3 - 8y^2 + 2y + 2 \quad \text{Ans.}$$

11)  $2x^4 + x^3 - 2x^2 + 5x + 7$  from  $a^3 - 3a^2 b + 4ab^2 + b^3$

**Solution:**

$$\Rightarrow -x^4 + 2x^3 + 6x^2 - 7x - 3 \quad \text{Ans.}$$

12)  $a^3 - 4a^2 b + 3ab^2 - b^3$  from  $a^3 - 3a^2 b + 4ab^2 + b^3$

**Solution:**

$$\Rightarrow a^2 b + ab^2 + 2ab^3 \quad \text{Ans.}$$

13) what should be added to  $2x^3 + x^2 + 2x$  to get the sum  $9x^3 + 4x^2 + 5x$  ?

**Solution:**

$$\Rightarrow 7x^3 + 3x^2 + 3x \quad \text{Ans.}$$

14) what should be added to  $6a^2 b^2 + 4b^2 c^2 + 3c^2$  to get the sum of  $11a^2 b^2 + 8b^2 c^2 + 7c^2$  ?

**Solution:**

$$\Rightarrow 5a^2 b^2 + 4b^2 c^2 + 4c^2 \quad \text{Ans.}$$

15) what should be added to  $4a^2 + 7b^2 + 9c^2 d^2$  so that the sum be  $14a^2 + 9b^2 + 12c^2 + 4d^2$  ?

**Solution:**

$$\Rightarrow 10a^2 + 2b^2 + 3c^3 + 3d^2 \quad \text{Ans.}$$

16) What should be subtracted from  $7a^2 b^2 + 8c$  to get  $3a^2 b^2 + 5c^2$  ?

**Solution:**

$$\Rightarrow 4a^2 b^2 + 3c^2 \quad \text{Ans.}$$

17) what should be subtracted from  $4c^2 - 2a^3 + 7a^2 + 6a$  to get a  $a^4 + 4a^3 + 3a^2 + 8a$ ?

**Solution:**

$$\Rightarrow 3a^4 - 6a^3 + 4a^2 - 2 \quad \text{Ans.}$$

18) What should be subtracted from  $x^2 y^2 + 3xy + y^2$  get  $2xy$ ?

**Solution:**

$$\Rightarrow x^2 y^2 + x y + y^2 \quad \text{Ans.}$$

19) Subtract the sum of  $2x + 3y$ ,  $4x - 2y$  from  $10x + 3y$ ?

**Solution:**

$$\Rightarrow 4x y + 4y \quad \text{Ans.}$$

20) Subtract from  $10x^2 + 3xy + 9y^2$  sum of  $3x^2 + 4xy + 5y^2$ ,  $4x^2 - 2xy - 4y^2$ ?

**Solution:**

$$\Rightarrow 3x + xy + 8y^2 \quad \text{Ans.}$$

### **Exercise 6.5**

Find the product of the following algebraic expression:

1)  $5a + 4b$  and 2

2)  $b^2, a^2, b^2, c^2$

**Solution:**

$$\Rightarrow 10a + 8b \quad \text{Ans}$$

**Solution:**

$$\Rightarrow a^2 b^4 c^2 \quad \text{Ans}$$

3)  $4x^2, 7y^2$

Solution:

$\Rightarrow 28x^2 y^2$

Ans

4)  $(-2x), (4xy)$

Solution:

$\Rightarrow -8x y$

Ans

5)  $(-3a^2), (7a^2 b^2)$

Solution:

$\Rightarrow -21 a^4 b^2$

Ans

6)  $(4x^2 y^2), (-5z^2)$

Solution:

$\Rightarrow -20x^2 y^2 z^2$

Ans

7)  $(-5p^2), (-7p^{10})$

Solution:

$\Rightarrow 35p^{12}$

Ans

8)  $2a^3, 4b^2, 5c^3$

Solution:

$\Rightarrow 40 a^3 b^2 c^3$

Ans

9)  $4a^2 b, 3ab^2, 10b^2 c^2$

Solution:

$\Rightarrow 120a^3 b^5 c^2$

Ans

10)  $6p^2, 7p^2, 8p^2$

Solution:

$\Rightarrow 336p^5 q$

Ans

11)  $(7x^3), (-12x^3), (4x^3)$

Solution:

$\Rightarrow -336x^9$

Ans

12)  $(-4a^2 x^2), (-3a^3 x^3), (-2a^4 x^4)$

Solution:

$\Rightarrow -24 a^9 x^9$

Ans

13)  $xy^2 z, x^2 yz^2, x^3 y^3 z^3$

**Solution:**

$\Rightarrow x^6 y^6 z^6$

Ans

14)  $12abc^2, 8a^3xy, 3x^2y^2z^3$

**Solution:**

$\Rightarrow 288 a^4 bc^2 x^3 y^3 z^3$

Ans

15)  $(-4x), (6xyz), (-2x^2y^2)$

**Solution:**

$\Rightarrow 48 x^4 y^3 z$

Ans

**Exercise 6.6**

Multiply together.

1)  $5a + 4b$  and 2

**Solution:**

$\Rightarrow 10a + 8b$  Ans

2)  $6x^2 - 5y^2$  and  $3xy$

**Solution:**

$\Rightarrow 18x^3 y - 15xy^3$  Ans

3)  $3a^2 - b^3$  and  $-2ab$

**Solution:**

$\Rightarrow -6a^4 b + 2ab^4$  Ans

4)  $3x^4 + x^2 y$  and  $2x^2 y^2$

Solution:

$$\Rightarrow 6x^6 y^2 + 2x^4 y^3 \quad \text{Ans}$$

5)  $4x^2 - y^2$  and  $-4x^3 y$

Solution:

$$\Rightarrow 16x^5 y + 4x^3 y^3 \quad \text{Ans}$$

6)  $3a^2 + 2ab$  and  $4ab$

Solution:

$$\Rightarrow 12a^3 b + 8a^2 b^2 \quad \text{Ans}$$

7)  $2x^3 - 3x^2 - 5$  and  $3x^2$

Solution:

$$\Rightarrow 6x^5 - 9x^4 - 15x^2 \quad \text{Ans.}$$

8)  $3x^2 - 5x - 2$  and  $-2x^2$

Solution:

$$\Rightarrow -6x^4 + 10x^3 + 4x^2 \quad \text{Ans.}$$

9)  $2a^2 - ab + a^2 c$  and  $2abc$

Solution:

$$\Rightarrow 4a^3 bc - 2a^2 b^2 c + 2a^3 b^2 \quad \text{Ans.}$$

10)  $2x^4 - x^3 y^2 + y^4$  and  $2x^2 y$

Solution:

$$\Rightarrow 4x^6 y - 2x^4 y^3 + 2x^2 y^5 \quad \text{Ans.}$$

11)  $5x^2 - 2xy^2 + y^3$  and  $3xy^2$

**Solution:**

$\Rightarrow 15x^2 - 2xy^2 + y^3$  and  $3xy$  Ans.

12)  $3a^3 - 5a^2b - 3ab^2$  and  $2ab$

**Solution:**

$\Rightarrow -6a^4b + 10a^3b^2 + 6a^2b^3$  Ans

13)  $3x^2 + 3xy + y^2$  and  $2y$

**Solution:**

$\Rightarrow 6x^2y + 6xy^2 - 2y^3$  Ans

14)  $2x^3 - 3x^2 - 5$  and  $-3x^2$

**Solution:**

$\Rightarrow -6x^5 + 9x^4 + 15x^2$  Ans

15)  $4x^3 - 8xy - 9y^2$  and  $2xy$

**Solution:**

$\Rightarrow 8x^4y - 16x^2y^2 - 18xy^3$  Ans

### **Exercise 6.7**

**Find the product of:**

1)  $(x + 3)(x + 8)$

**Solution:**

$\Rightarrow x^2 + 11x + 24$  Ans

2)  $(2a + 3)(3a + 4)$

**Solution:**

$\Rightarrow 6a^2 + 17a + 12$  Ans

3)  $(x - 7y)(x - 3y)$

**Solution:**

$$\Rightarrow x^2 - 10xy + 21y^2 \quad \text{Ans}$$

4)  $(x - 6y)(x + 5y)$

**Solution:**

$$\Rightarrow x^2 - xy - 30y^2 \quad \text{Ans}$$

5)  $(a + 5b)(2a - 2b)$

**Solution:**

$$\Rightarrow 2a^2 + 10b^2 \quad \text{Ans}$$

6)  $(2x^2 + 5y^2)(2x^2 + 5y^2)$

**Solution:**

$$\Rightarrow 4x^4 + 20x^2y^2 + 25y^4 \quad \text{Ans}$$

7)  $(4x^2 - 3y^2)(5x^2 - 6y^2)$

**Solution:**

$$\Rightarrow 20x^4 - 39x^2y^2 + 18y^4 \quad \text{Ans}$$

8)  $(2a^2 - 3c^2)(7a^2 - 5c^2)$

**Solution:**

$$\Rightarrow 14a^4 - 31a^2c^2 + 15c^4 \quad \text{Ans}$$

9)  $(2x^2 + 3y^2)(5x^2 + 2y^3)$

**Solution:**

$$\Rightarrow 10x^4 + 6y^5 \quad \text{Ans}$$

10)  $(4x^2 + 3y^2)(3x^2 + 4y^2)$

**Solution:**

$$\Rightarrow 12x^4 + 25x^2y^2 + 12y^4 \quad \text{Ans}$$

**Exercise 6.8**

**Divide:**

1)  $9x^4 y^3$  by  $3x^2 y$

**Solution:**

$$\Rightarrow 3x^2 y^2 \quad \text{Ans}$$

2)  $20x^7 y^2$  by  $5x^4 y^2$

**Solution:**

$$\Rightarrow 4x^3 \quad \text{Ans}$$

3)  $25x^3 y^7 z^4$  by  $5xyz^2$

**Solution:**

$$\Rightarrow 5x^2 y^6 z^2 \quad \text{Ans}$$

4)  $28a^6 b^5 c^4$  by  $7a^4 b^3 c$

**Solution:**

$$\Rightarrow 4a^2 b^2 c^3 \quad \text{Ans}$$

5)  $42x^2 y^2 z^2$  by 6

**Solution:**

$$\Rightarrow 7x^2 y^2 z^2 \quad \text{Ans}$$

6)  $40p^6 q^6$  by  $8p^4 q^3$

**Solution:**

$\Rightarrow sp^2 q^2$  Ans

7)  $39x^4 y^5$  by  $-3x^2 y^5$

**Solution:**

$\Rightarrow -12x^2 y^2$  Ans

8)  $-52x^2 y^4 z^{10}$  by  $13x^2 y^3 z^7$

**Solution:**

$\Rightarrow -4yz^2$  Ans

9)  $81a^2 b^6 c^6$  by  $-9a^3 b^2 a^4$

**Solution:**

$\Rightarrow -9a^3 b^4 c^2$  Ans

10)  $21x^7 y^4$  by  $-7x^5 y^2$

**Solution:**

$\Rightarrow 3x^3 y^2$  Ans

**Exercise 6.9**

**Divide**

1)  $6x^2 + 4xy$  by  $2x$

**Solution:**

$\Rightarrow 3x + 2y$  Ans

2)  $8a^3 b^2 - 12a^4 b^3$  by  $2ab$

**Solution:**

$\Rightarrow 4a^2 b - 6a^3 b^2$  Ans4

3)  $12x^2y - 9xy^2$  by  $x^2y$

Solution:

$\Rightarrow 4x - 3y$  Ans

4)  $16x^5 + 8x^4$  by  $4x^2$

Solution:

$\Rightarrow 4x^3 + 2x^2$  Ans

5)  $a^5 b^2 c^4 - a^3 b^3 c^3$  by  $abc$

Solution:

$\Rightarrow a^4 bc^3 - a^2 b^2 c^2$  Ans

6)  $4x^5 y^7 + 6x^4 y^3$  by  $2x^2 y^2$

Solution:

$\Rightarrow 2x^3 + 3x^2y$  Ans

7)  $a^3 x^3 - a^2 bx^2 + a^3 x^5$  by  $ax$

Solution:

$\Rightarrow a^3 x^3 + abx + a^2 x^2$  Ans

8)  $2a^2 b^2 - 4ab - 8b^3$  by  $2b$

Solution:

$\Rightarrow a^2 b - 2a - 4b^2$  Ans

9)  $4a^7 b^5 + 2a^6 b^4 + 8a^5 b^4 + 12 a^4 b^2$  by  $2a^3 b^2$

Solution:

$\Rightarrow 2a^4 b^3 + 3a^3 b^2 + 4a^2b + 6a$  Ans

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10)  $20a^3 b^3 c^3 + 30a^2 b^2 c^2 + 15 abc^3 + 10 abc$  by  $5abc$

Solution:

$$\Rightarrow 4a^2 b^2 + 6abc + 3c^2 + 2 \quad \text{Ans}$$

**Exercise 6 .10**

Find the solution set of

1)  $a + 9 = 15$

Solution:

$$\Rightarrow \{ 6 \} \quad \text{Ans}$$

2)  $2x + 6 = 18$

Solution:

$$\Rightarrow \{ 6 \} \quad \text{Ans}$$

3)  $3x - 7 = 17$

Solution:

$$\Rightarrow \{ 8 \} \quad \text{Ans}$$

4)  $3a - 8 = 24$

Solution:

$$\Rightarrow \{ 8 \} \quad \text{Ans}$$

5)  $8x + 4 = 60$

Solution:

$$\Rightarrow \{ 7 \} \quad \text{Ans}$$

6)  $5y - 10 = 15$

Solution:

$$\Rightarrow \{ 5 \} \quad \text{Ans}$$

7)  $6z + 12 = 36$

Solution:

$$\Rightarrow \{ 4 \} \quad \text{Ans}$$

8)  $7p - 11 = 66$

Solution:

$$\Rightarrow \{ 11 \} \quad \text{Ans}$$

9)  $10 + 6 = 56$

Solution:

$$\Rightarrow \{ 5 \}$$

Ans

10)  $9x - 9 = 72$

Solution:

$$\Rightarrow \{ 9 \}$$

Ans

11)  $\frac{9+7}{3} = 5$

Solution:

$$\Rightarrow \{ 8 \}$$

Ans

12)  $3x - \frac{1}{2} = \frac{21}{2}$

Solution:

$$\Rightarrow \{ \frac{11}{3} \}$$

Ans

13)  $\frac{4x+3}{3} = 9$

Solution:

$$\Rightarrow \{ 6 \}$$

Ans

14)  $\frac{3x}{2} - \frac{8}{3} = \frac{1}{2}$

Solution:

$$\Rightarrow \{ \frac{19}{9} \}$$

Ans

15)  $\frac{6y}{4} + \frac{7}{2} = \frac{1}{8}$

Solution:

$$\Rightarrow \{ \frac{-24}{12} \}$$

Ans

16)  $3(2x + 3) = -15$

Solution:

$$\Rightarrow \{ -4 \}$$

Ans

17)  $\frac{4x+12}{8} = 8$

Solution:

$$\Rightarrow \{ 13 \}$$

Ans

18)  $8(a + 4) = 0$

Solution:

$$\Rightarrow \{ -4 \}$$

Ans

$$19) \quad \frac{3x}{2} - \frac{4}{5} = \frac{19}{5}$$

Solution:

$$\Rightarrow \{ 2 \}$$

Ans

$$20) \quad 2 ( 2x - 3 ) = 28$$

Solution:

$$\Rightarrow \{ 5 \}$$

Ans

**Exercise 6.11**

**Find the solution set of:**

$$1) \quad 5x - 4 = 2x + 11$$

Solution:

$$\Rightarrow \{ 5 \}$$

Ans

$$2) \quad 2x = 7 + 3x$$

Solution:

$$\Rightarrow \{ -7 \}$$

Ans

$$3) \quad 7y + 3 = y + 18$$

Solution:

$$\Rightarrow \{ \frac{5}{2} \}$$

Ans

$$4) \quad x + 3 = 18 - 3x$$

Solution:

$$\Rightarrow \{ \frac{15}{4} \}$$

Ans

$$5) \quad 5(a + 1) + 3(a - 1) = 5$$

Solution:

$$\Rightarrow \{ \frac{3}{8} \}$$

Ans

6)  $3(1 - y) + 4(y - 5) = 10$

Solution:

$\Rightarrow \{27\}$  Ans

7)  $3x - 4 = 14 - 3x$

Solution:

$\Rightarrow \{3\}$  Ans

8)  $6x - 4x = 3x + 84$

Solution:

$\Rightarrow \{12\}$  Ans

9)  $5(x + 2) + 3(x + 4) = 26$

Solution:

$\Rightarrow \{\frac{1}{2}\}$  Ans

10)  $3x + 7 + 6x = x + 28 + 5x$

Solution:

$\Rightarrow \{7\}$  Ans

### Exercise 6.12

1) A certain number plus 10 is 25 find the number.

Solution:

$\Rightarrow 15$  Ans

2) I think of a number, twice the number plus 7 gives the result 17. Find the number.

Solution:

$\Rightarrow 5$  Ans

3) When 3 is subtracted from four times a number if gives 21 as result find the number.

**Solution:**

$$\Rightarrow 6 \quad \text{Ans}$$

4) I think of a number, multiply it by 7 and subtract 10; the result is 25 find the number?

**Solution:**

$$\Rightarrow 5 \quad \text{Ans}$$

5) 8 years ago, the age of sadia was 7 years find her present age.

**Solution:**

$$\Rightarrow 5 \quad \text{Ans}$$

6) Bushra will be 15 years old, 2 years hence. How old is bushra now?

**Solution:**

$$\Rightarrow 13 \text{ years} \quad \text{Ans}$$

7) if 9 is add to here times a number, the result is 30. Find the number.

**Solution:**

$$\Rightarrow 7 \quad \text{Ans}$$

8) My present age is 40 years. Now old small I be after 12 years and what was my age 14 years ago?

### Solution:

$$\Rightarrow 52 \quad \text{Ans}$$

9) I think a number, double it and subtract 14; the result 30, find the number.

### Solution:

⇒ 22 Ans

10) I think of a number, divide it by 2 two and subtract 7 the result is 8. Find the number.

### Solution:

$$\Rightarrow 30 \quad \text{Ans}$$

**Chapter 7****GEOMETRY****Exercise 7.1**

6) The length of the bases of a trapezium are 9cm and 14cm and its altitude is 6cm, find the area of the trapezium?

**Solution:**

$$\Rightarrow \frac{1}{2} ( 9 + 14 ) ( 6 )$$

$$\frac{1}{2} ( 23 ) ( 6 )$$

$$\frac{1}{2} ( 138 ) = 69 \text{ sq cm.} \quad \text{Ans}$$

7) The length of the bases of a trapezium are 3 cm and 8cm and its altitude is 2 cm. find the area of the trapezium?

**Solution:**

$$\Rightarrow \frac{1}{2} ( 3 \times 8 ) ( 2 )$$

$$\frac{1}{2} ( 11 ) ( 2 )$$

$$\frac{1}{2} ( 22 ) 11 \text{ sq cm.} \quad \text{Ans}$$

**Exercise 7.2**

1) Find the circumference of a circle whose radius is 63 cm.

**Solution:**

$$\begin{aligned}\Rightarrow C &= 2 \pi r \text{ formula} \\ C &= 2 \times \pi \times 63 \\ C &= 126 \pi \text{ cm} \\ \text{Using } \pi &\approx 3.14159 \\ C &= 126 \times 3.14159 \approx 395.84 \text{ cm} \quad \text{Ans}\end{aligned}$$

2) Find the circumference of a circle when its diameter is 147 m long.

**Solution:**

$$\begin{aligned}\Rightarrow \text{Formula: } C &= \pi d \\ C &= \pi \times 147 \\ C &= 147 \pi \text{ m} \\ C &= 147 \times 3.14159 = 461.81 \text{ m} \quad \text{Ans}\end{aligned}$$

3) The radius of a circular building is 714 m. How much time will be taken to move around the building with a speed of 3 km/h?

**Solution:**

$$\begin{aligned}\Rightarrow C &= 2 \pi r = 2 \pi (714) = 1428 \pi \text{ m} \\ C &= 1428 \times 3.14159 \approx 4487.11 \text{ km} \\ \text{Time} &= \frac{4487.11}{3} \approx 1.4957 \text{ hours} \\ 1.4957 \times 60 &\approx 89.74 \text{ m} \quad \text{Ans}\end{aligned}$$

4) A plate 2.2 m long is put on the rim of the bottom of a drum. Find the length of diameter of the circular bottom of the drum?

**Solution:**

$$\Rightarrow 2.2 = \pi d$$
$$d = \frac{2.2}{\pi}$$
$$d \approx 0.70\text{m} \quad \text{Ans}$$

5) How many revolutions will a wheel of radius 35cm make in covering a distance of 660m?

**Solution:**

$$\Rightarrow \text{Radius} = 35 \text{ cm} = 0.35\text{m}$$
$$2 \pi (0.35) \approx 2.2 \text{ m}$$
$$\frac{660}{2.2 \pi} \approx \frac{660}{2.198} = 300 \quad \text{Ans}$$

6) The minute hand of a clock is 14m long. How much distance will the minute hand cover in?

1) One hour?

**Solution:**

$$\Rightarrow 2 \pi r = 2 \pi (14) = 28 \pi = 87.96\text{m} \quad \text{Ans.}$$

2) Three hours?

**Solution:**

$$\Rightarrow 3 \times 28 \pi = 84 \pi = 263.89\text{m} \quad \text{Ans}$$

3) Twenty four hours?

**Solution:**

$$\Rightarrow \text{Distance} = 24 \times 28 \pi = 672 \pi = 2111.5 \text{ m} \quad \text{Ans}$$

4) Half on hour?

Solution:

$$\Rightarrow \text{Distance} = \frac{1}{2} \times 28 \pi = 14 \pi = 43.98\text{m} \quad \text{Ans}$$

**Exercise 7.3**

1) Find the area of the circular region, when the radius is:

1) 28 cm

Solution:

$$\Rightarrow A = \pi (28)^2, A = \pi (784) \\ A \approx 2463.008 \text{ cm}^2 \quad \text{Ans}$$

2) 4.9m

Solution:

$$\Rightarrow A = \pi (4.9)^2, A = \pi (24.01) \\ A \approx 75.43 \text{ m}^2 \quad \text{Ans}$$

3) 42cm

Solution:

$$\Rightarrow A = \pi (42)^2, A = \pi (1764) \\ A = 5541.769 \text{ cm}^2 \quad \text{Ans}$$

4) 1.4m

Solution:

$$\Rightarrow A = \pi (1.4)^2, A = \pi (1.96) \\ A = 6.1575 \text{ m}^2 \quad \text{Ans}$$

2) Find the diameter of the circular region when its area is:

1) 154 sq.cm

**Solution:**

$$\Rightarrow 154 = \pi r^2$$

$$r^2 = \frac{154}{\pi} r^2$$

$$r = 7\text{cm}$$

$$\text{diameter} = 2r = 14\text{cm}$$

Ans

2) 2464sq cm

**Solution:**

$$\Rightarrow 2464 = \pi r^2$$

$$r^2 = \frac{2464}{\pi} \approx 784$$

$$r = 28\text{ cm}$$

$$\text{diameter} = 2r \approx 56\text{ cm.}$$

3)  $3850 = \pi r^2$

**Solution:**

$$\Rightarrow 3850 = \pi r^2$$

$$r^2 = \frac{3850}{\pi} \approx 122$$

$$r = 35\text{m, diameter} = 2r \approx 70\text{m}$$

Ans

4) 124.74 sq cm

**Solution:**

$$\Rightarrow 124.74 = \pi r^2$$

$$r^2 = \frac{124.74}{\pi} \approx 391$$

$$r = 6.3\text{m} . \text{diameter} = 2r \approx 12.6\text{ cm}$$

Ans

3) Find the area of a circular ground if diameter is 126m long.

**Solution:**

$$\Rightarrow 126 / 2 = 63 \text{ m}$$
$$\text{Area} = \pi r^2 = \pi (63)^2 \approx 12474 \text{ sq.m} \quad \text{Ans}$$

4) A circular fountain is built in the center of crossing its radius in 3m. what is the area of the fountain?

**Solution:**

$$\Rightarrow \pi (3)^2 = 9 \pi = 28.27 \text{ sq.m} \quad \text{Ans}$$

5) A table cover is made 70 cover a round dinning table. The radius of the table cover is 1m long. What is the area of table cover.

**Solution:**

$$\Rightarrow \pi (1)^2 = \pi \approx 3.14 \text{ sq.m} \quad \text{Ans}$$

6) The diameter of a circular part is 35m. find the cost of planting grass at the rate of Rs. 15.20 per square meter.

**Solution:**

$$\Rightarrow 34 / 2 = 17.5 \text{ m}$$
$$\pi (17.5)^2 \approx 962 \text{ sq.m}$$
$$932.11 \times 15.20 = 14614.15 \text{ Rs} \quad \text{Ans}$$

7) The length of an arm of a fan as measured from tis center is 10cm. what will be the area moved through by the arm in one revolution?

**Solution:**

$$\Rightarrow \pi (10)^2 = 100 \pi = 3.14 \cdot 16 \text{ sq.m} \quad \text{Ans}$$

**Exercise 7.4**

In each of the following the radius of the base of the cylinder and its height is given, find its volume.

1) Radius = 2.8m , Height = 5m

**Solution:**

$$\Rightarrow v = \pi (2.8)^2 (8) = 123.15 \text{ m}^3 \quad \text{Ans}$$

2) Radius = 1.05m, height = 2.5m

**Solution:**

$$\Rightarrow v = \pi (1.05)^2 (2.5) \approx 8.66 \text{ m}^3 \quad \text{Ans}$$

3) The diameter of a cylindrical tank is 13m long and its height is 14m. find the volume of the tank.

**Solution:**

$$\Rightarrow v = \pi r^2 h = \pi (6.5)^2 (14) = 504 \pi \approx 1583.36 \text{ m}^3$$

Ans.

4) The diameter of a cylindrical tank is 14m long and its volume is 1540 cubic meters, find its height.

**Solution:**

$$\Rightarrow v = \pi r^2 h, 1540 = \pi (7)^2 h$$

$$h = \frac{1540}{49\pi} = 10 \text{ m} \quad \text{Ans.}$$

5) If the radius of the mouth of 3.5m deep a cylindrical pit is 1.5m, how much will be needed to fill its?

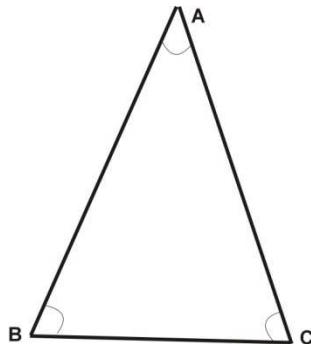
**Solution:**

$$\Rightarrow V = \pi r^2 h = \pi (1.5)^2 (3.5) = 7.875 \approx 24.74 \text{ m}^3$$

Ans

**Exercise 7.5**

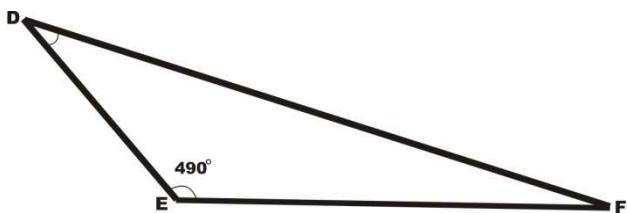
1) Measure the angles and lengths of the sides of the following triangle:



**Solution:**

$$\Rightarrow m\angle BAC = 50^\circ$$
$$m\angle ACB = 60^\circ$$
$$m\angle CBA = 70^\circ$$

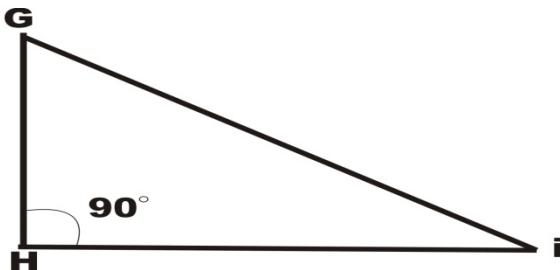
$$m\angle BAC + m\angle ACB + m\angle CBA =$$
$$80^\circ + 60^\circ + 70^\circ = 180^\circ \quad \text{Ans}$$



2)

**Solution:**

$$\begin{aligned}
 \Rightarrow m \angle DEF &= 60^\circ \\
 m \angle EFD &= 60^\circ \\
 m \angle FDE &= 70^\circ \\
 m \angle DEF + m \angle EFD + m \angle FDE &= 190^\circ \\
 60^\circ + 60^\circ + 70^\circ &= 190^\circ
 \end{aligned}
 \quad \text{Ans}$$

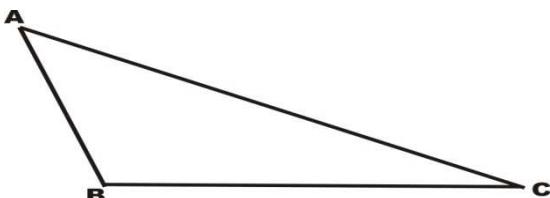


3)

**Solution:**

$$\begin{aligned}
 \Rightarrow m \angle GHI &= 90^\circ \\
 m \angle HIG &= 50^\circ \\
 m \angle IGH &= 40^\circ \\
 m \angle GHI + m \angle HIG + m \angle IGH &= 180^\circ \\
 90^\circ + 50^\circ + 40^\circ &= 180^\circ
 \end{aligned}
 \quad \text{Ans}$$

2) Measure the angles of the triangle given below and verify that the sum of the measure of all angle in every triangles is  $108^\circ$ .

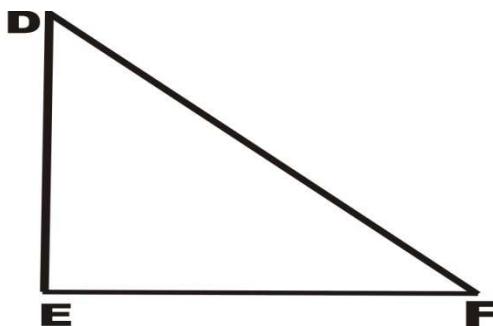


1)

**Solution:**

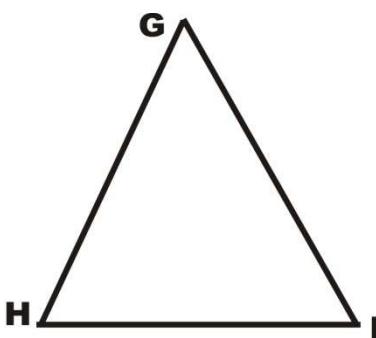
$$\begin{aligned}\Rightarrow \quad m < CAB &= 50^\circ \\ \Rightarrow \quad m < ABC &= 60^\circ \\ \Rightarrow \quad m < BCA &= 70^\circ \\ m < CAB + m < ABC + m < BCA & \\ 50^\circ + \quad 60^\circ + \quad 70^\circ + & \quad 180^\circ \\ & \text{Ans}\end{aligned}$$

2)

**Solution:**

$$\begin{aligned}\Rightarrow \quad m < DEF &= 50^\circ \\ \Rightarrow \quad m < EFD &= 50^\circ \\ \Rightarrow \quad m < FDE &= 80^\circ \\ m < DEF + m < EFD + m < FDE & \\ 50^\circ + \quad 50^\circ + \quad 80^\circ + & \quad 180^\circ \\ & \text{Ans}\end{aligned}$$

3)

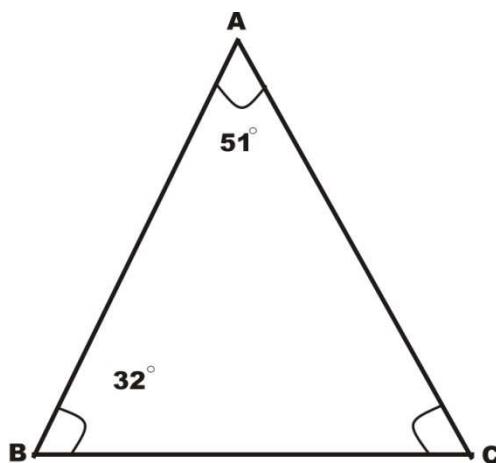


**Solution:**

$$\begin{aligned}
 \Rightarrow m\angle GHI &= 90^\circ \\
 m\angle HIG &= 60^\circ \\
 m\angle IGH &= 30^\circ \\
 m\angle GHI + m\angle HIG + m\angle IGH &= 180^\circ \\
 90^\circ + 60^\circ + 30^\circ &= 180^\circ
 \end{aligned}
 \quad \text{Ans}$$

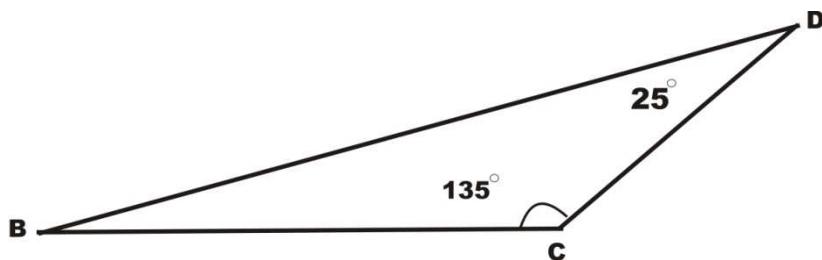
3) Measure those angle of the triangle given below which are not indicated. Also find their measures without actually measuring them.

1)

**Solution:**

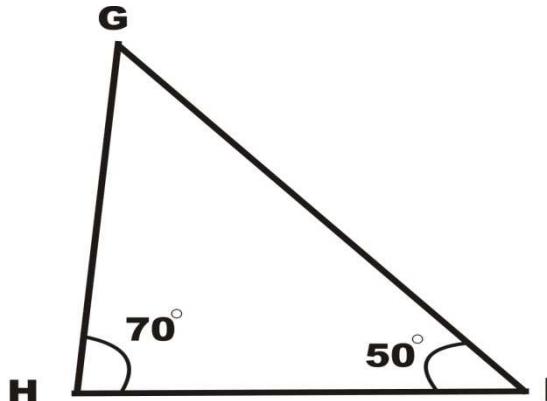
$$\begin{aligned}
 \Rightarrow 180^\circ &= m\angle A + m\angle B + m\angle C \\
 180^\circ &= 51^\circ + 32^\circ + m\angle C \\
 180^\circ &= 83^\circ + m\angle C \\
 180^\circ - 83^\circ &= m\angle C \\
 97^\circ &= m\angle C
 \end{aligned}
 \quad \text{Ans}$$

2)

Solution:

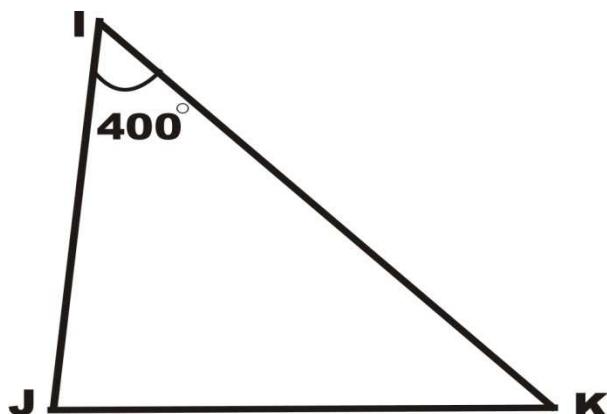
$$\begin{aligned}\Rightarrow 180^\circ &= m\angle B + m\angle C + m\angle D \\ 180^\circ &= m\angle B + 135^\circ + 25^\circ \\ 180^\circ &= m\angle B + 160^\circ \\ 160^\circ - 180^\circ &= m\angle B \\ 20^\circ &= m\angle B\end{aligned}\quad \text{Ans}$$

3)

Solution:

$$\begin{aligned}\Rightarrow 180^\circ &= m\angle G + m\angle H + m\angle I \\ 180^\circ &= m\angle G + 70^\circ + 50^\circ \\ 180^\circ &= m\angle G + 120^\circ \\ 120^\circ - 180^\circ &= m\angle G \\ 60^\circ &= m\angle G\end{aligned}\quad \text{Ans}$$

4) Find the measure off an active angle of a right angled triangle when the measure of the other active angle given.



Solution:

$$\begin{aligned}\Rightarrow 180^\circ &= m\angle I + m\angle J + m\angle K \\ 180^\circ &= 48^\circ + m\angle K \\ 180^\circ &= 48^\circ + m\angle J + m\angle K \\ 132^\circ &= m\angle J + m\angle K \quad \text{Ans}\end{aligned}$$

2)  $m\angle L = 48^\circ$ .

Solution:

$$\begin{aligned}\Rightarrow 180^\circ &= m\angle L + m\angle M + m\angle N \\ 180^\circ &= 48^\circ + m\angle M + m\angle N \\ 180^\circ - 48^\circ &= m\angle M + m\angle N \\ 132^\circ &= m\angle M + m\angle N \quad \text{Ans}\end{aligned}$$

3)  $m\angle P = 55^\circ$

**Solution:**

$$\Rightarrow 180^\circ = m\angle O + m\angle P + m\angle R$$

$$180^\circ = m\angle O + 55^\circ + 90^\circ$$

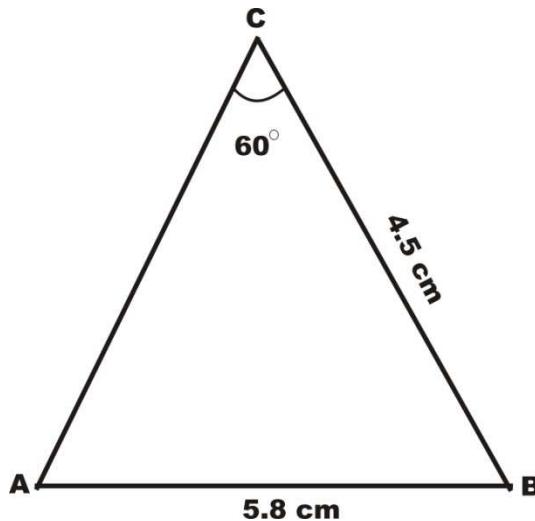
$$180^\circ = m\angle O + 145^\circ$$

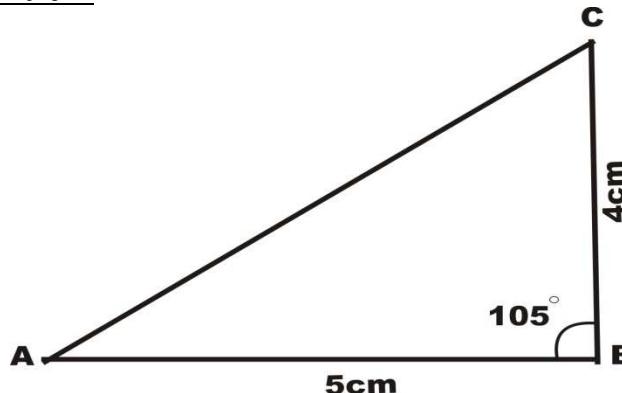
$$180^\circ - 145^\circ = m\angle O \quad \text{Ans}$$

**Exercise 7.6**

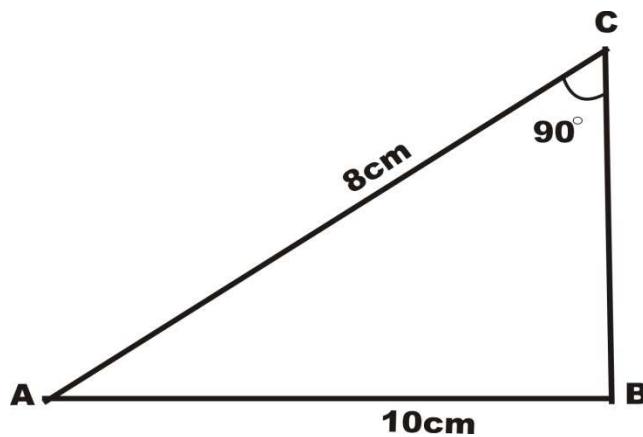
1) Construct a triangle in each of the following when two its sides and the included angle is given.

1)  $m\angle A = 5.8\text{cm}$ ,  $m\angle B = \overline{4.5\text{cm}}$ ,  $m\angle C = 60^\circ$

**Solution:**

2)  $m\angle A = \text{Sum}$ ,  $m\angle B = 4\text{cm}$ ,  $m\angle C = 105^\circ$ **Solution:**

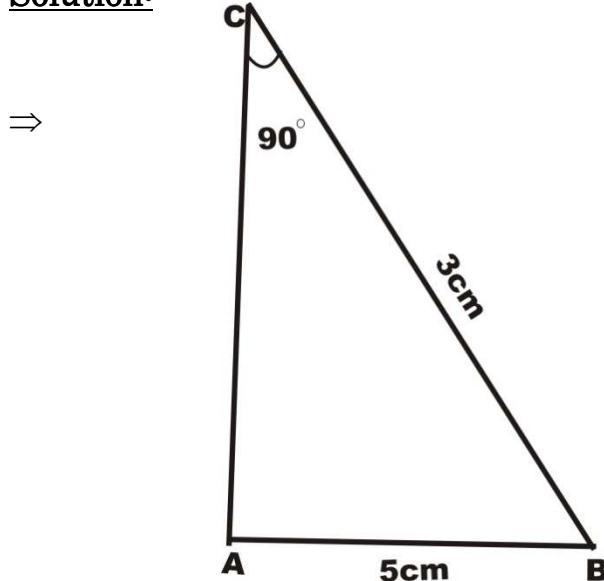
Ans

2) Construct a right triangle ABC when hypotenuse and one of the adjacent is given below ( $m\angle C = 90^\circ$ )1)  $m\angle A = 10\text{cm}$ ,  $m\angle C = 8\text{cm}$ **Solution:** $\Rightarrow$ 

Ans

2)  $m\angle A = 5\text{cm}$ ,  $m\angle B = 3\text{cm}$

Solution:



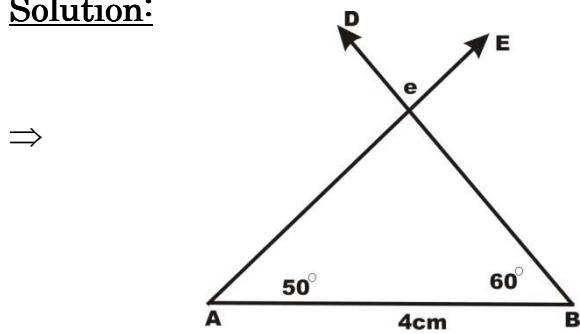
Ans

Exercise 7.7

1) Construct triangle ABC when the following are two angles and the included side:

1)  $m\angle A = 50^\circ$ ,  $m\angle B = 60^\circ$ , and  $mAB = 4\text{cm}$ .

Solution:

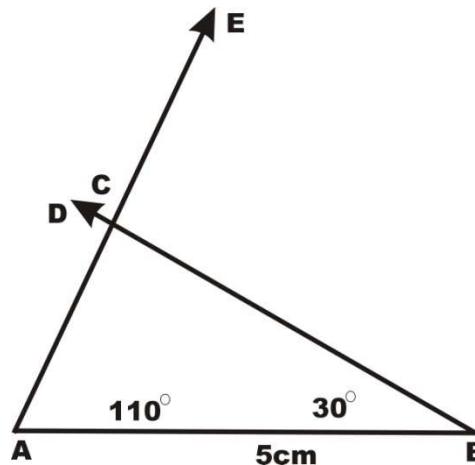


Ans

2)  $m\angle A = 110^\circ$ ,  $m\angle B = 30^\circ$ , and  $mAB = 5\text{cm}$

Solution:

$\Rightarrow$



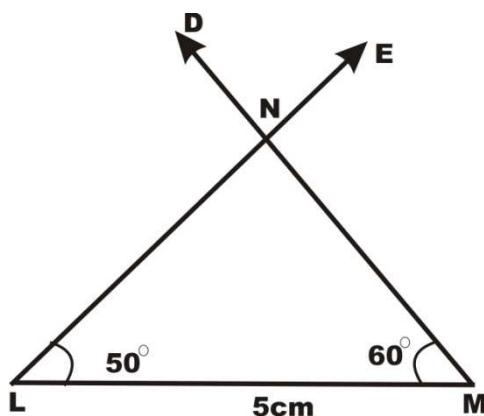
Ans

2) Construct triangle LMN when the measure of two angles E the measure of a side opposite one of these angle are given:

1)  $m\angle L = 50^\circ$ ,  $m\angle M = 60^\circ$  and  $mLN = 4\text{cm}$

Solution:

$\Rightarrow$

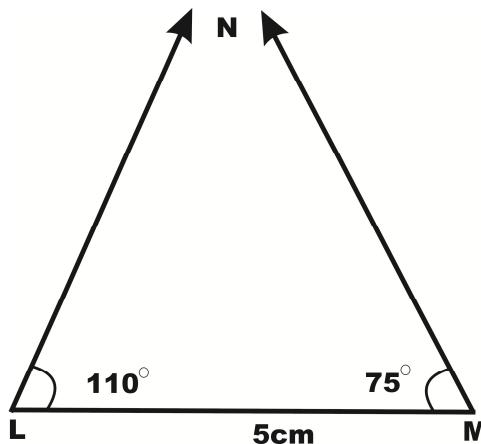


Ans

2)  $m\angle L = 110^\circ$ ,  $m\angle M = 75^\circ$  and  $m\overline{LN} = 5\text{cm}$ .

**Solution:**

$\Rightarrow$



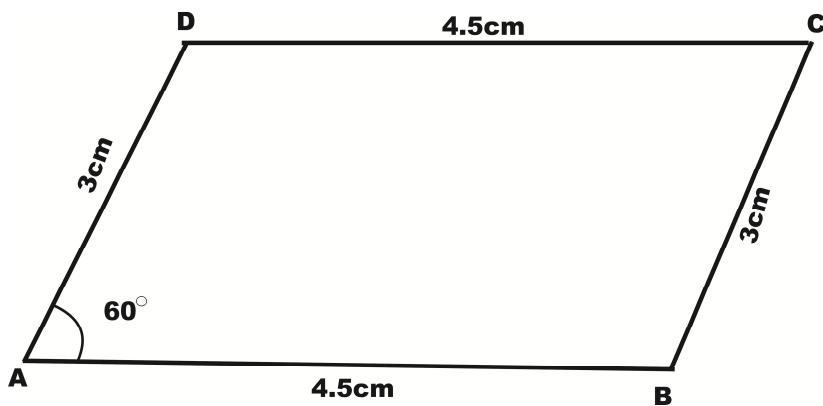
Ans

**Exercise 7.8**

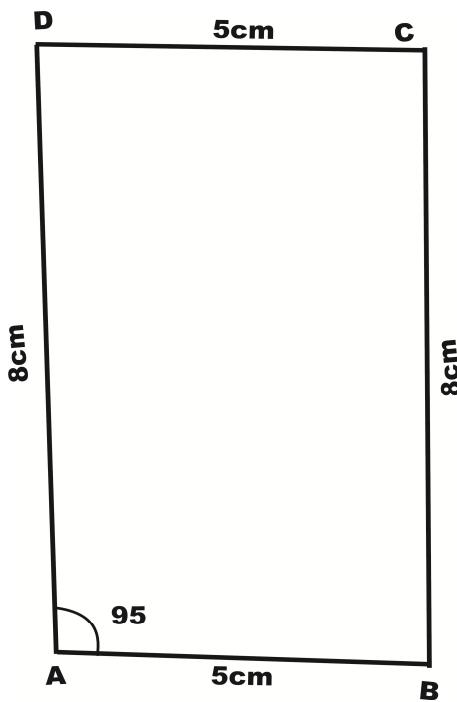
1) Construct parallelogram ABCD when.

1)  $m\overline{AB} = 4.5\text{cm}$ ,  $m\overline{AD} = 3\text{cm}$ ,  $m\angle A = 60^\circ$

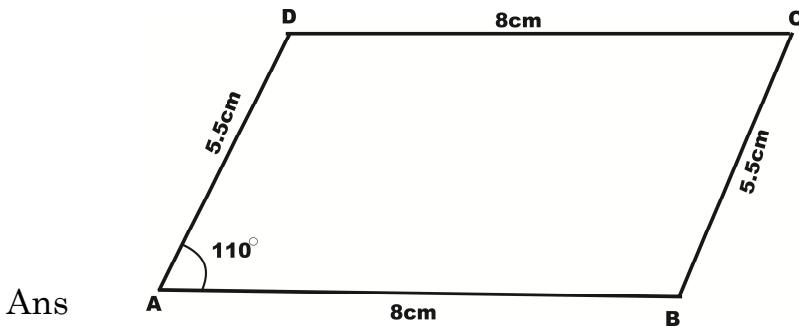
**Solution:**



Ans

2)  $m\overline{AB} = 5\text{cm}$ ,  $m\overline{AD} = 8\text{cm}$ ,  $m\angle A = 85^\circ$ Solution:3)  $m\overline{AB} = 8\text{cm}$ ,  $m\overline{AD} = 5.5\text{cm}$  and  $m\angle A = 110^\circ$ 

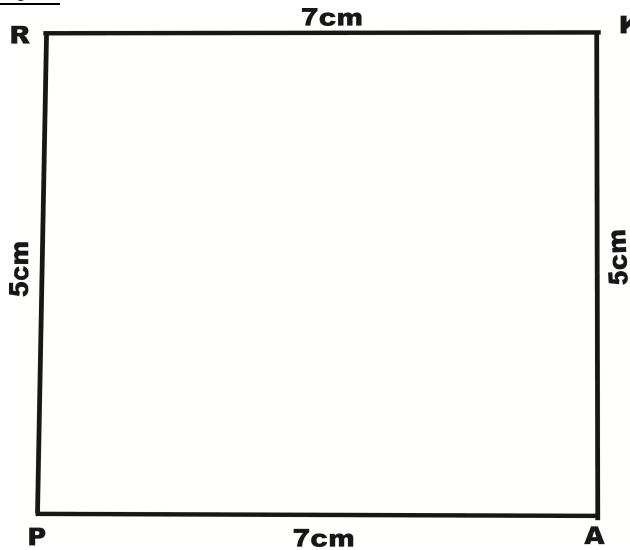
Ans

Solution:

Ans

2) Draw a parallelogram PARK when.  
1)  $m\overline{PA} = 7\text{cm}$ ,  $m\overline{PR} = 5\text{cm}$  and  $m\overline{AK} = 6\text{cm}$

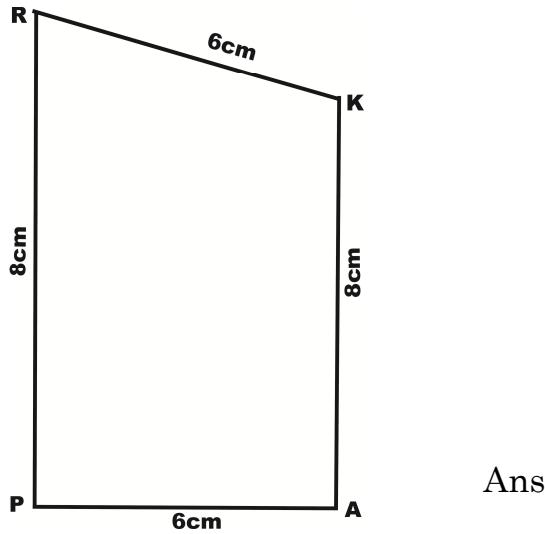
**Solution:**



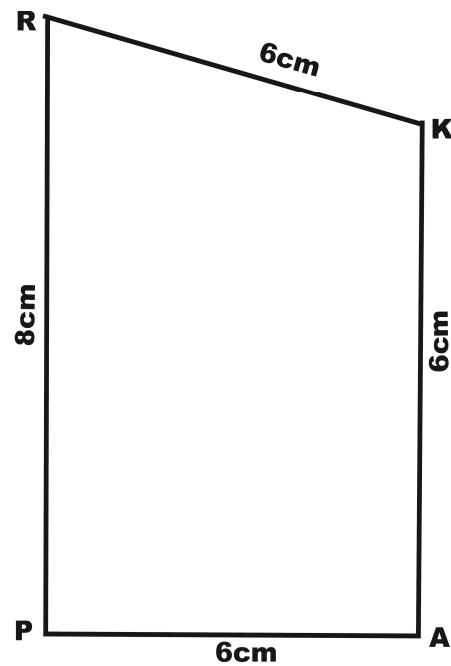
Ans

2)  $m\overline{PA} = 4.3\text{cm}$ ,  $m\overline{PK} = 7.7\text{cm}$  and  $m\overline{AK} = 6.2\text{cm}$

**Solution:**



Ans

3)  $mPA = 6\text{cm}$  ,  $mPK = 8\text{cm}$  and  $mAK = 6\text{cm}$ **Solution:**

Ans

## Chapter 8

## INFORMATION HANDLING

**Exercise 8.1**

1) Represent the following data by a pie-graph.

**Solution:**

Item	Area Cultivate	Measure of the angles of the sectors representing the expenses
Wheat	800 acre	$800/300 \times 360 = 960^\circ$
Grain	200 acre	$200/300 \times 360 = 240^\circ$
Barley	40 acre	$40/300 \times 360 = 48^\circ$
Pluses	120 acre	$120/300 \times 360 = 144^\circ$
Grass	40 acre	$40/300 \times 360 = 48^\circ$
Total	300	$1440^\circ$

2) Represent the following data by pie graph. Ans

Distance	Population	Measure of the angle of the sectors representing the expenses.
1	14 lac	$14/36 \times 360 = 140$
2	10 lac	$10/36 \times 360 = 100$
3	6 lac	$6/36 \times 360 = 60$
4	2 lac	$2/36 \times 360 = 20$
5	4 lac	$4/36 \times 360 = 40$
Total	36	$360^\circ$ Ans

3) Represent the following data by a pie-graph.

**Solution:**

Item	Expenditure	Measure of the angle of the sectors representing the expenses.
Food	Rs. 4000	$4000/7000 \times 360 = 205 : 71$
Education	Rs. 500	$5000/7000 \times 360 = 25 : 71$
Utility Bills	Rs. 1000	$1000/7000 \times 360 = 51 : 42$
Miscelleneaus	Rs. 1500	$1500/7000 \times 360 = 77 : 142$
Expenses		
Total	7000	359.982 Ans

### **Exercise 8.2**

1) following are marks obtained by 22 students in math's test.  
 10,9,8,5,12,6,14,10,7,13,6,5,16,19,14,13,12,11,4,0,7,2. Taking 4 as the span of the class internal, arrange the date by tally method. Write down the frequencies also.

**Solution:**

Mark obtained	Tally Marks	Frequency
0 – 3	1111	4
4 – 7	1111	4
8 – 11	11	7
12 – 15		5
16 – 19	11	2
Total		22 Ans

2) Following table represent the marks obtained by students in mathematics.

Marks Obtained	Number of Students
1 – 10	5
11 – 20	16
21 – 30	3
31 – 40	8
41 – 50	7
Total	39

Ans

3) Keeping above the table in view answer following questions:

1) How many students are there?

❖ 39 Ans

2) How many class intervals are there?

❖ 1 – 10, 11 – 20, 21 – 30, 31 – 40, 41 – 50,  
Ans

3) What are class boundaries of class internal?

1-10 : 0.5 -10.5, 11-20 : 10.5 – 20.5 , 21-30 : 20.5 - 30.5, 31-40 : 30.5 -40.5 , 41.-50 : 40.5 – 50.5 Ans

4) What are class marks {mid point} of class internal?

$1-10 = (1+10)/2 = 5.5$  ,  $11-20 = (11+20)/2 = 15.5$ ,  
 $21 - 30 (21+30)/2 = 25.5$   $31-40 = (31 + 40)/2 = 35.5$  ,  $41-50 = (41+50)/2 = 45.5$  Ans

5) What is size of each class interval?

$10 - 1 + 1 = 10$  Ans